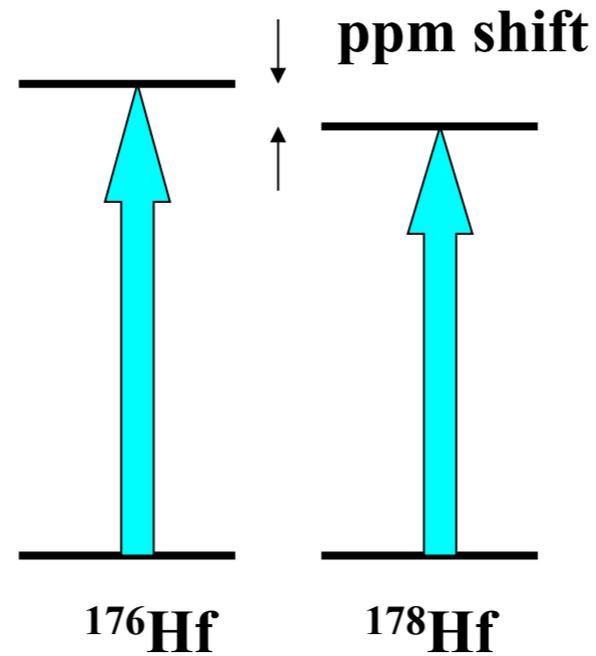


**Ground state properties and
moments via laser
spectroscopy**

Jon Billowes

RILIS lasers at ISOLDE

Isotope shift of an atomic transition



Two components: mass shift (nuclear recoil) and *volume shift*

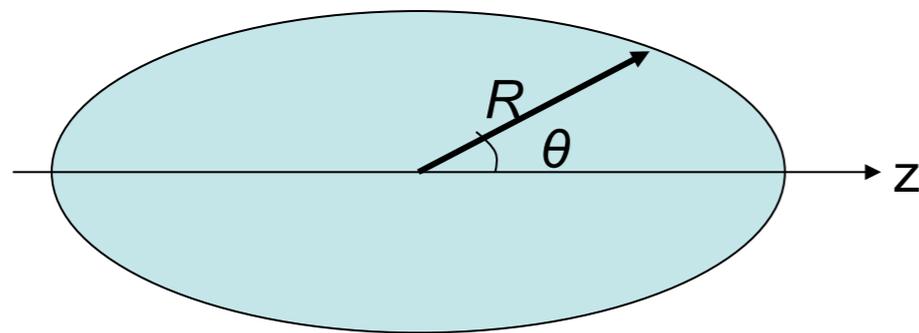
Analysis of *volume shift* yields the change in nuclear mean square charge radius,

$$\delta\langle r^2 \rangle$$

Nuclear size, deformation

$$\delta\langle r^2 \rangle = \delta\langle r^2 \rangle_{\text{sph}} + \langle r^2 \rangle_{\text{sph}} \frac{5}{4\pi} \delta\langle \beta_2^2 \rangle$$

volume dynamic deformation

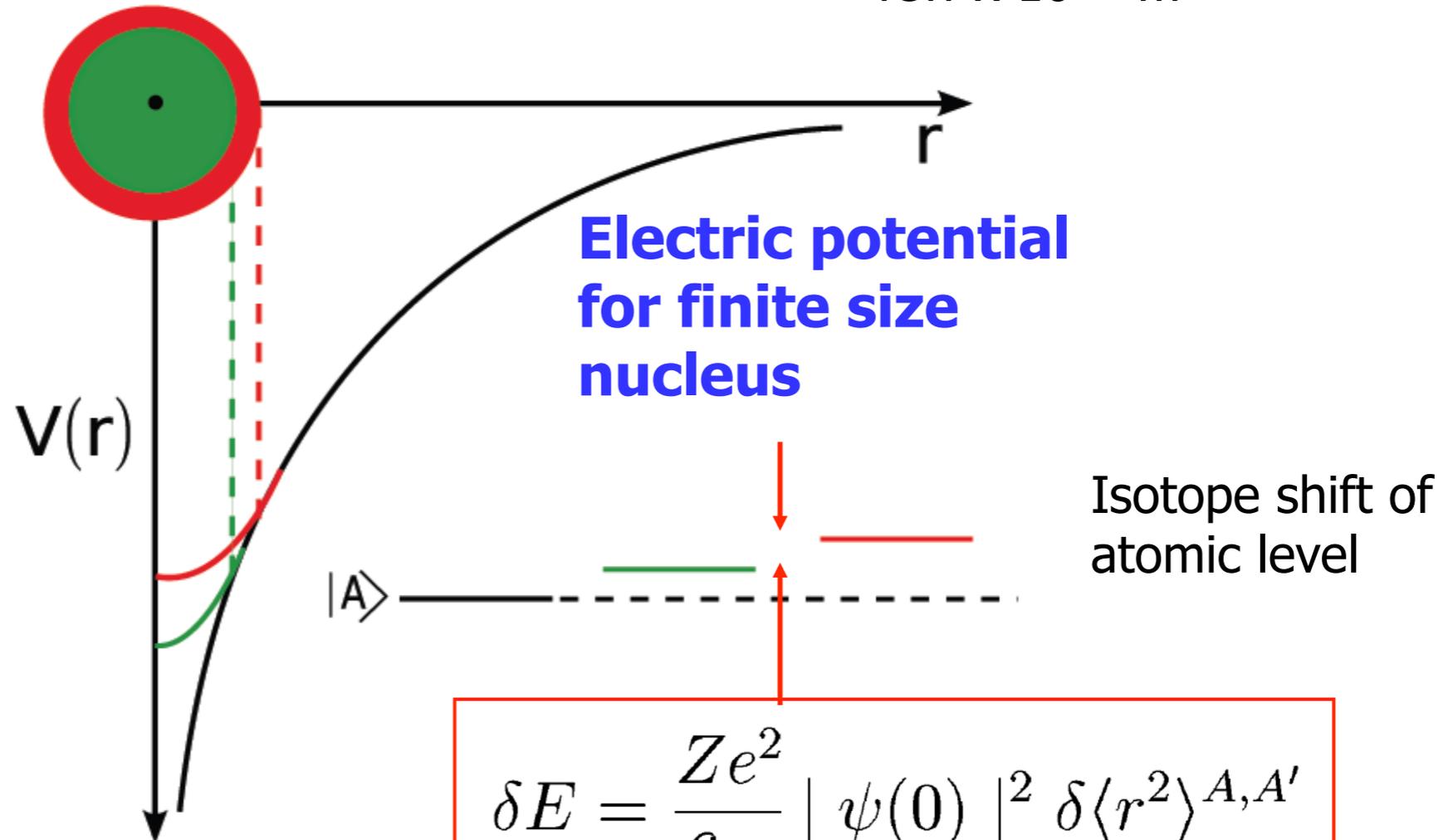


$$R = R_0 (1 + \beta_2 Y_{2,0}(\theta, \varphi))$$

The volume shift component

Nuclear radius:
few $\times 10^{-15}$ m

Electron radius:
few $\times 10^{-10}$ m

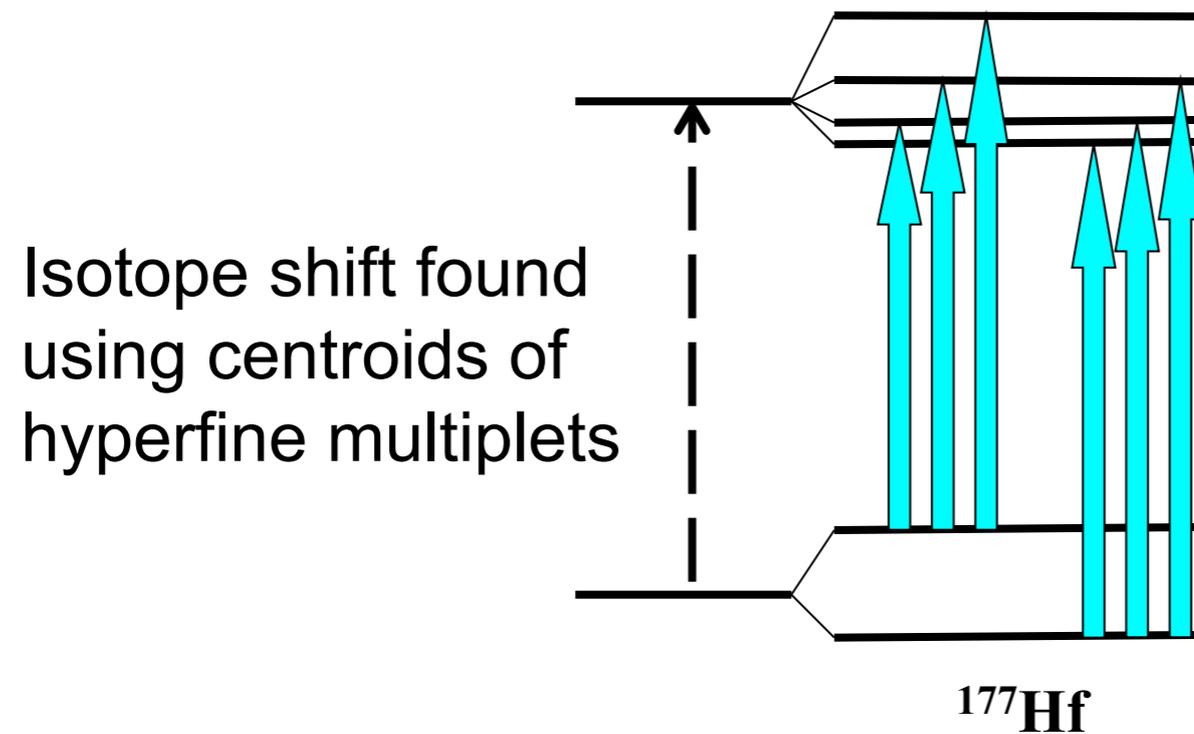


$$\delta E = \frac{Ze^2}{6\epsilon_0} |\psi(0)|^2 \delta \langle r^2 \rangle_{A,A'}$$

electron density at the nucleus

Hyperfine structure of an atomic transition

Analysis yields A and B hyperfine factors of both atomic states



$$A = \frac{\mu_I B_e(0)}{IJ} \quad B = e Q_s \left\langle \frac{\partial^2 V_e}{\partial z^2} \right\rangle$$



Nuclear spin I

Magnetic moment μ

Quadrupole moment Q_s

Without a definite spin, none of the other nuclear parameters can be deduced

Isotope shift \longrightarrow $\langle \beta_2^2 \rangle$ Dynamic deformation

Q_s \longrightarrow $\langle \beta_2^2 \rangle$ Static deformation

$\langle \beta_2^2 \rangle \approx \langle \beta_2 \rangle^2$ in well-deformed nuclei

Isotope shift = (normal + specific) mass shift + volume shift

$$\delta \langle r^2 \rangle^{A' A}$$

Approximate magnitudes for $\Delta A = 2$

Element	Transition	Normal	Specific	Volume	Doppler
----------------	-------------------	---------------	-----------------	---------------	----------------

Broadening

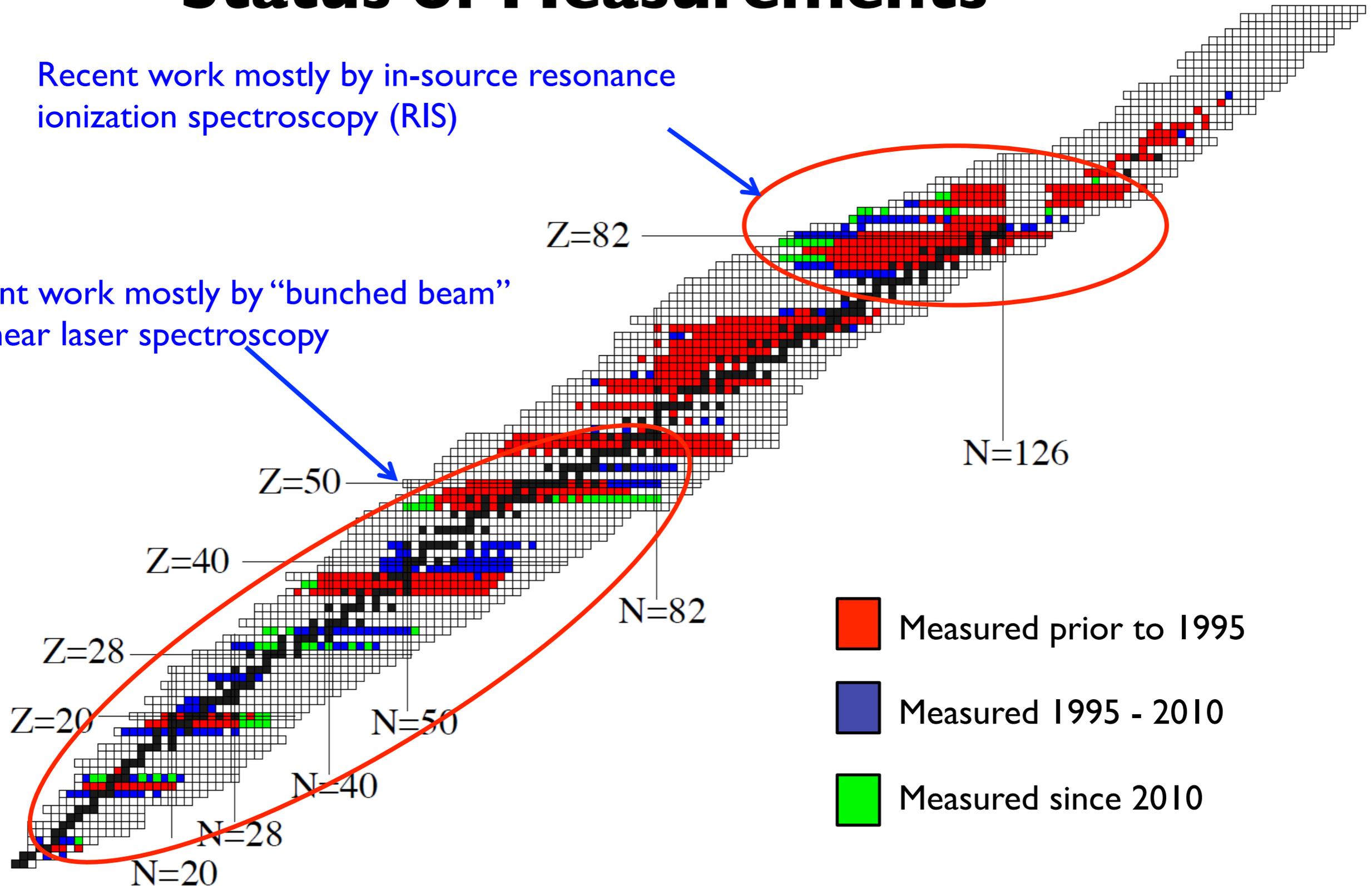
$_{11}\text{Na}$	3s – 3p	550 MHz	200 MHz	-10 MHz	1400 MHz
$_{70}\text{Yb}$	6s – 6p	20 MHz	< 20 MHz	-1500 MHz	500 MHz

(isomers: no mass shift to worry about)

Laser spectroscopy – Status of Measurements

Recent work mostly by in-source resonance
ionization spectroscopy (RIS)

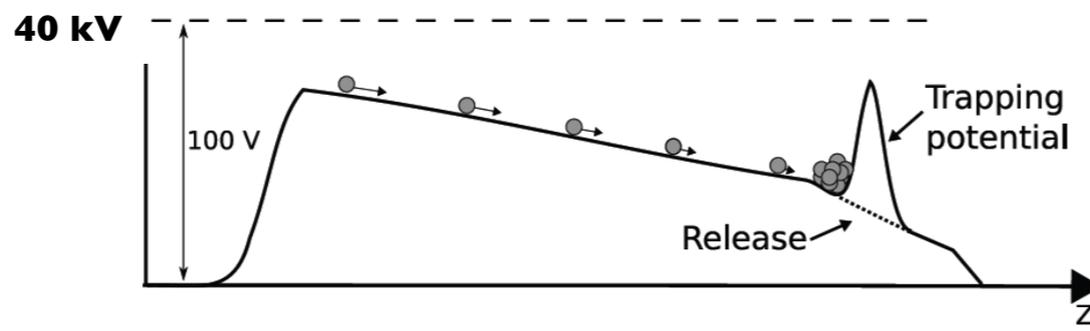
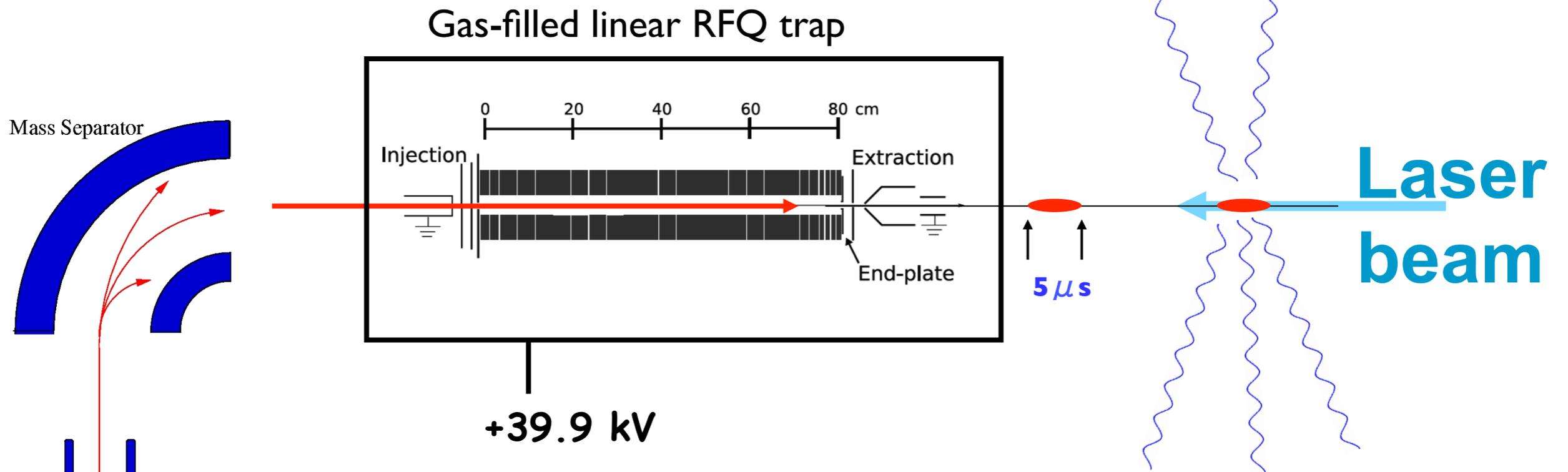
Recent work mostly by “bunched beam”
collinear laser spectroscopy



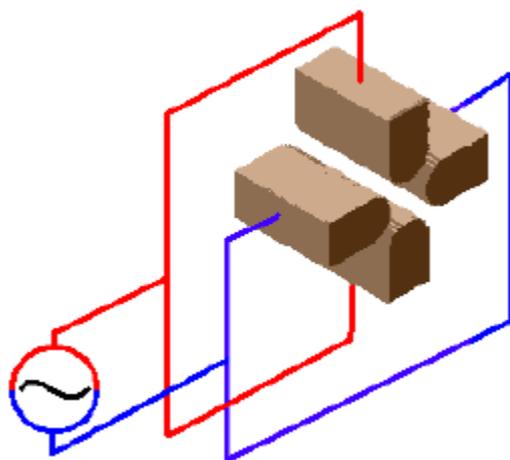
- Measured prior to 1995
- Measured 1995 - 2010
- Measured since 2010

**Updated plot provided by Bradley Cheal from 2010
review (B. Cheal & K.T. Flanagan J. Phys. G 37 (2010) 113101)**

Bunched-beam collinear laser spectroscopy (Doppler-free, greatly reduced background)



**TRIUMF ion beam cooler/
buncher**



Radioactive beam
ion source

+40 kV

Acceleration
region

Extractor
Electrodes

40 kV

100 V

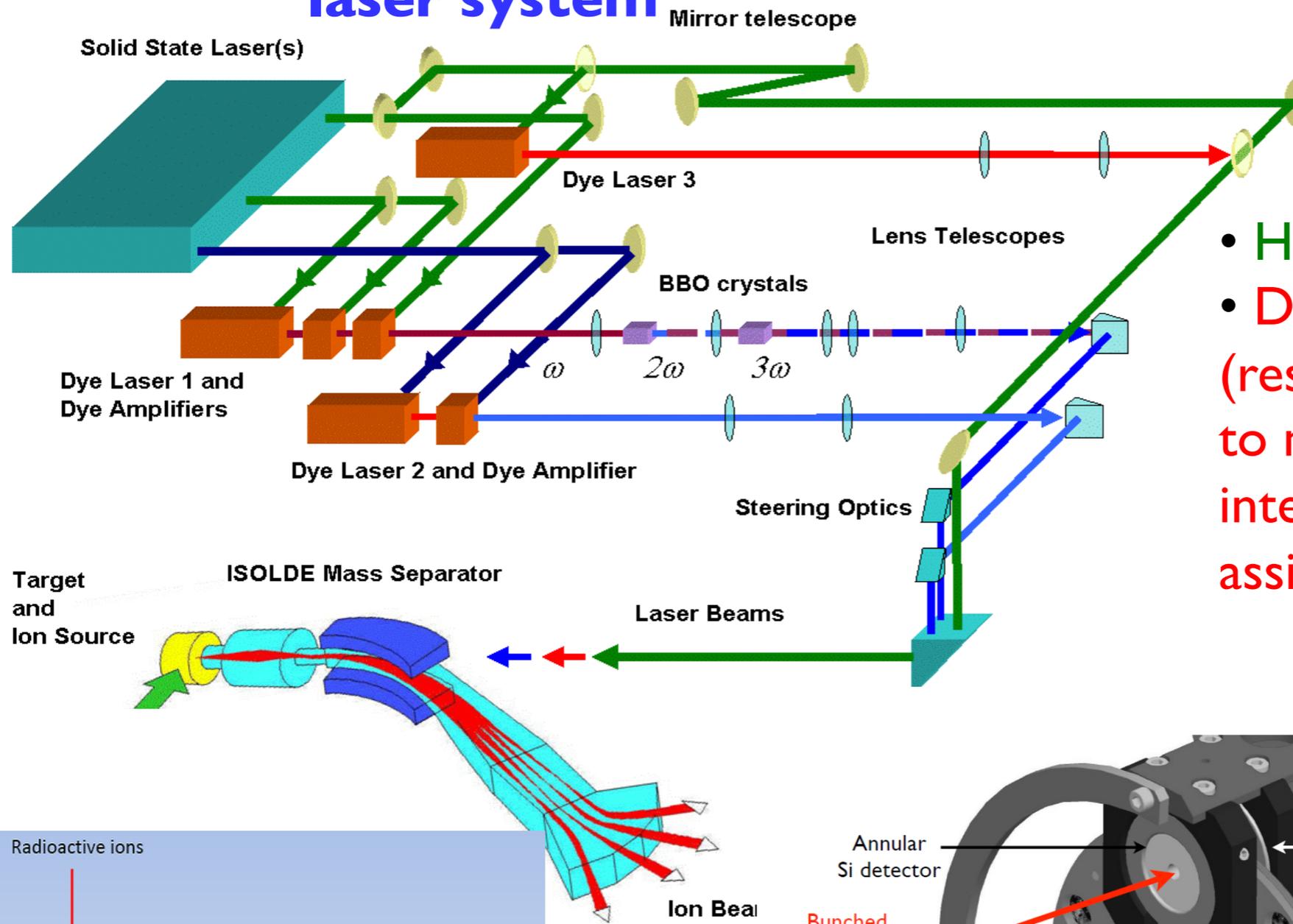
+39.9 kV

5 μs

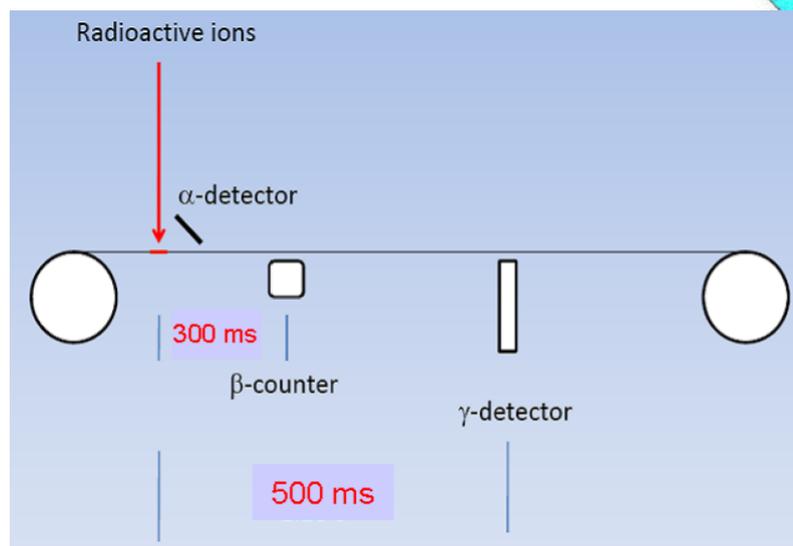
Laser
beam



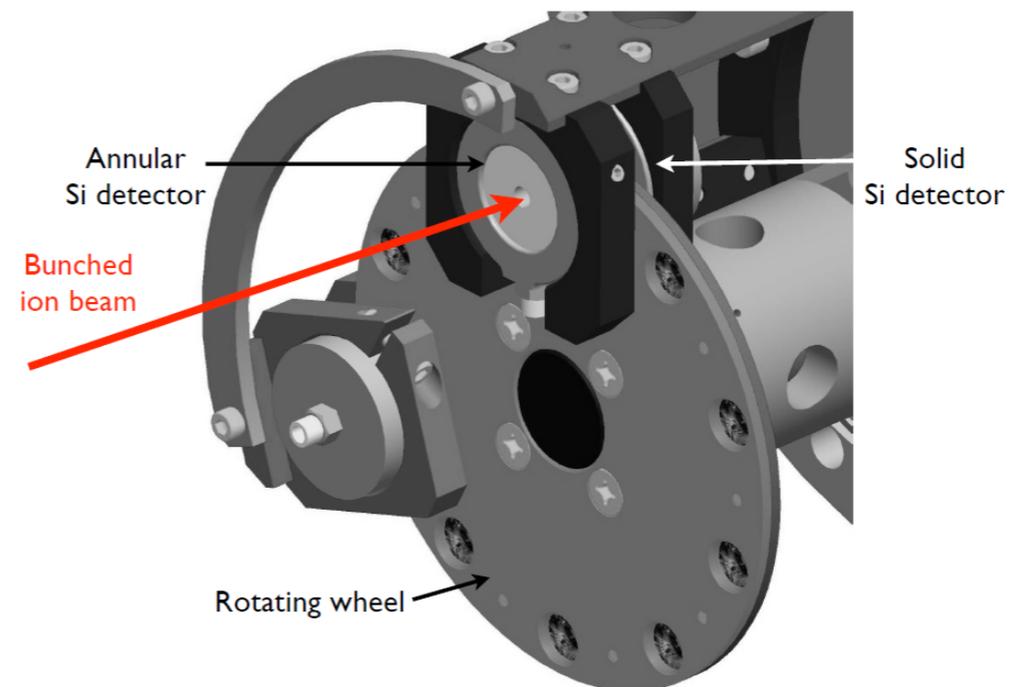
Resonance Ionization Spectroscopy with RILIS Pulsed laser system



- High sensitivity
- Doppler broadened (resolution usually too low to measure quadrupole interaction or make spin assignments)

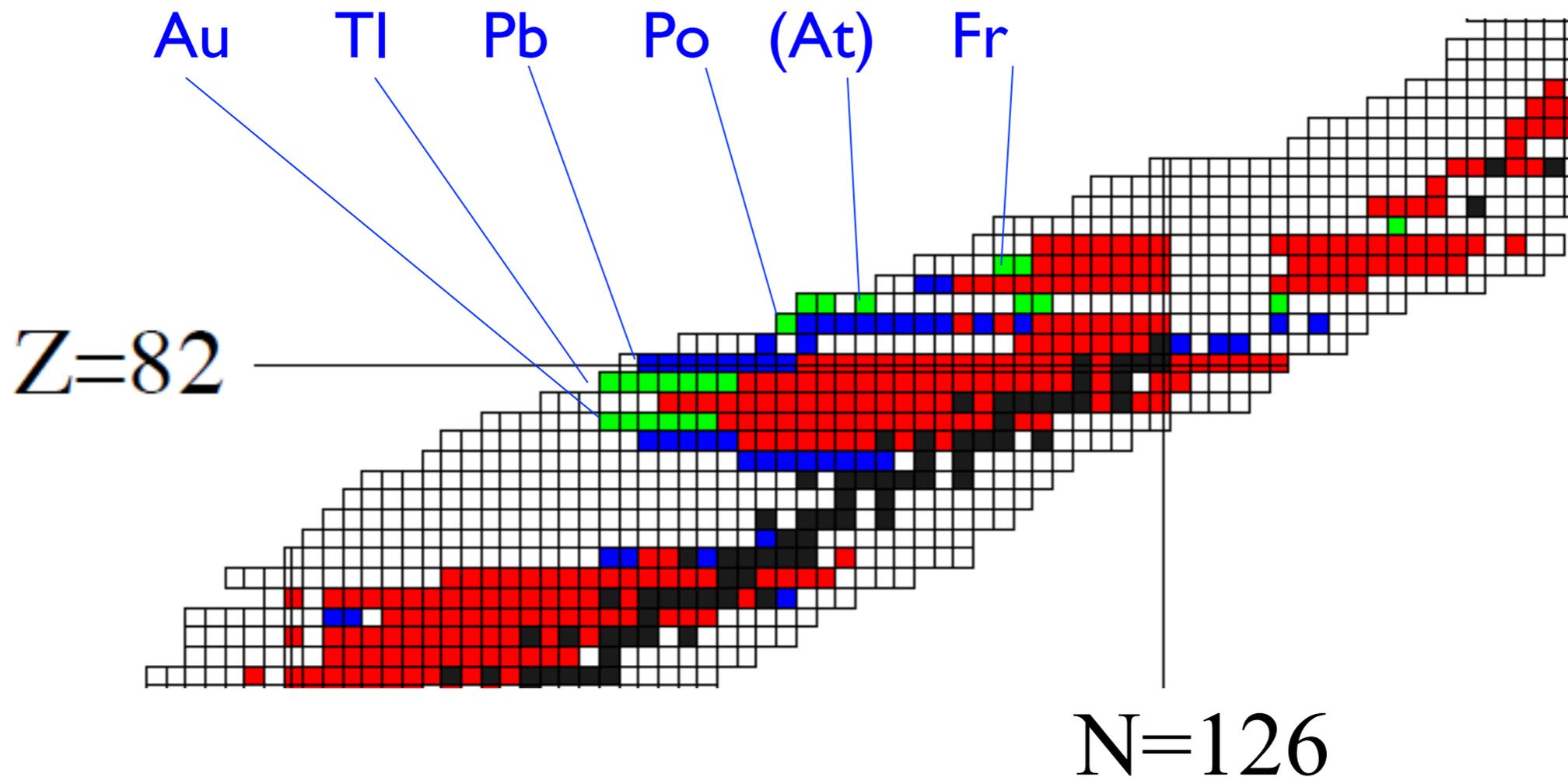


IRIS (Gatchina) tape station



“windmill” detection system (ISOLDE)

Charge radii systematics near $Z = 82$

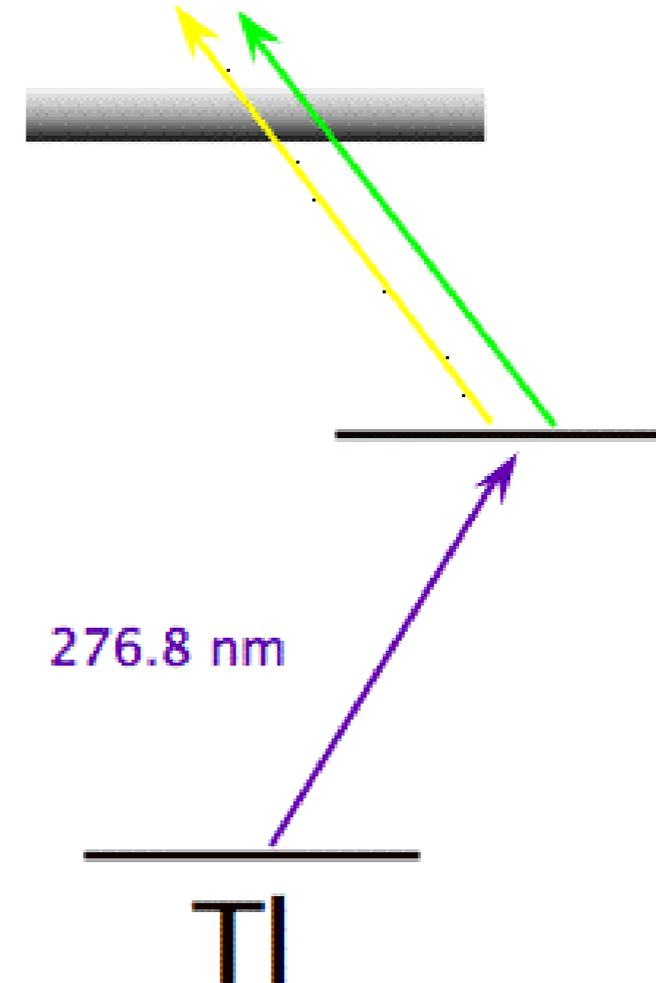


(Astatine RIS schemes developed by ISOLDE (RILIS) and TRIUMF (TRILIS) in preparation for in-source spectroscopy measurements at ISOLDE in September 2012)

Neutron-deficient Tl isotopes and isomers:

Collaboration between  and the IRIS facility, PNPI, Gatchina

Measured isotope shifts and magnetic moments on 276.8 nm transition (unable to measure small quadrupole interaction)



IRIS measurements:

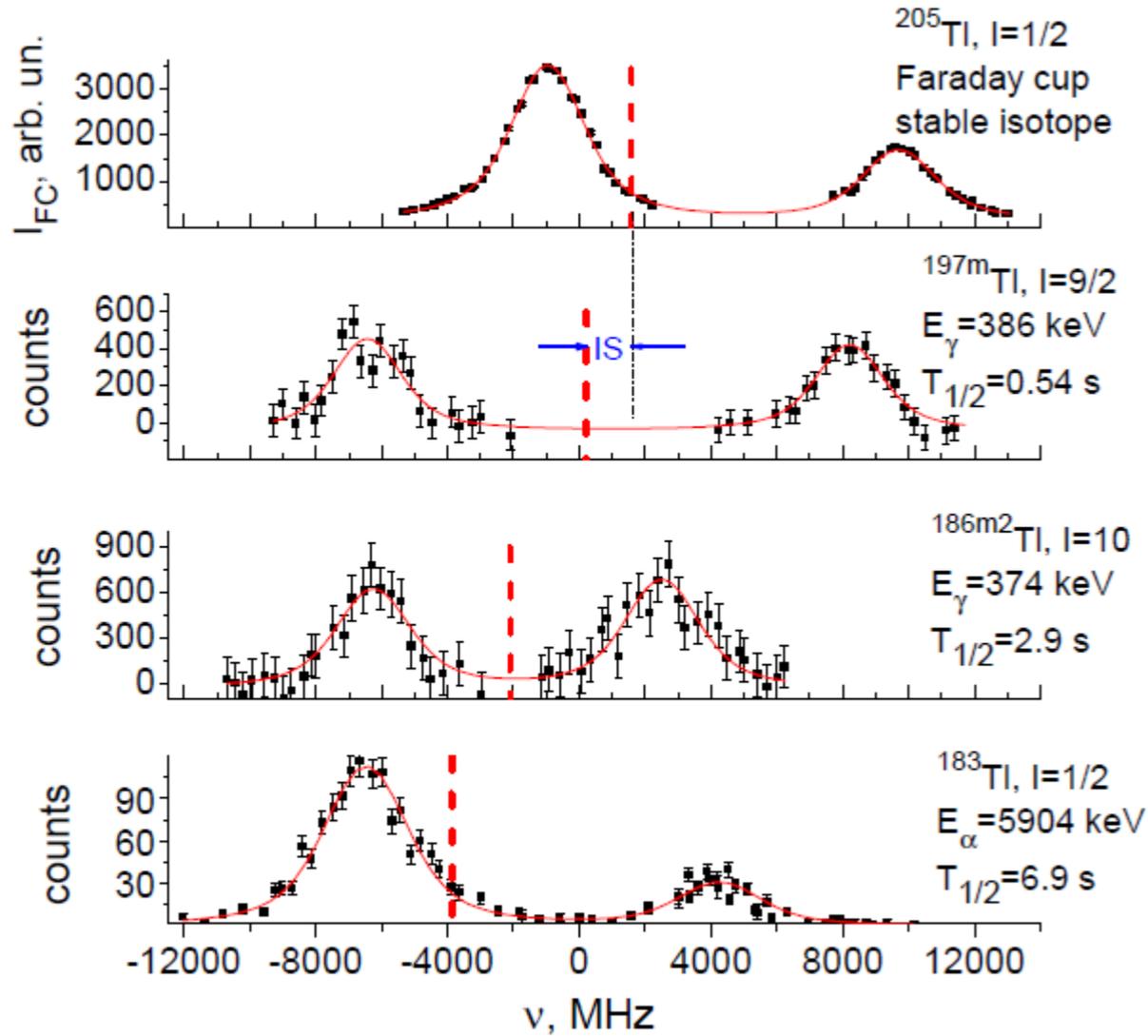
$A = 183 - 195, 197, 203, 205, 207$

King plot calibration of 277nm
atomic factors

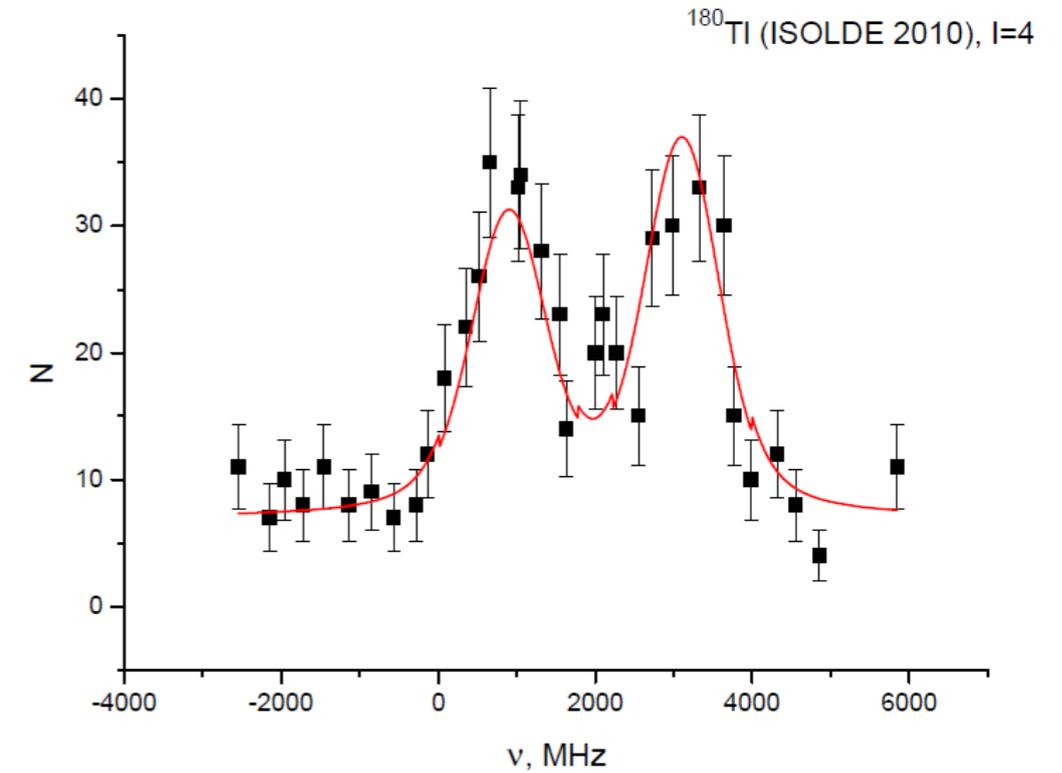
ISOLDE measurements:

$A = 179 - 184$

Thallium spectra



IRIS Spectra

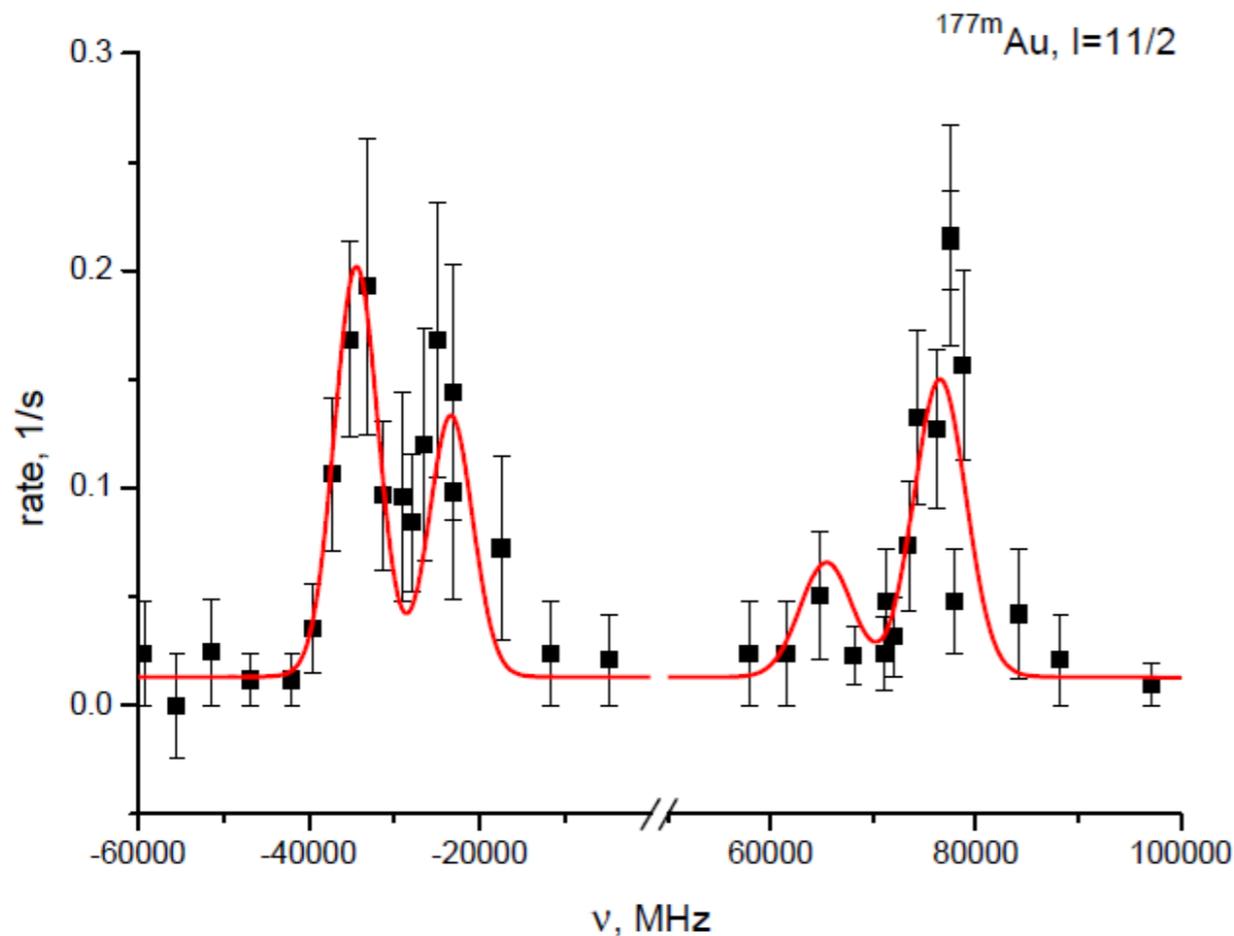


ISOLDE Spectrum

Data Courtesy Andreyev & Barzakh

Au isotopes: (ISOLDE/RILIS and PNPI)

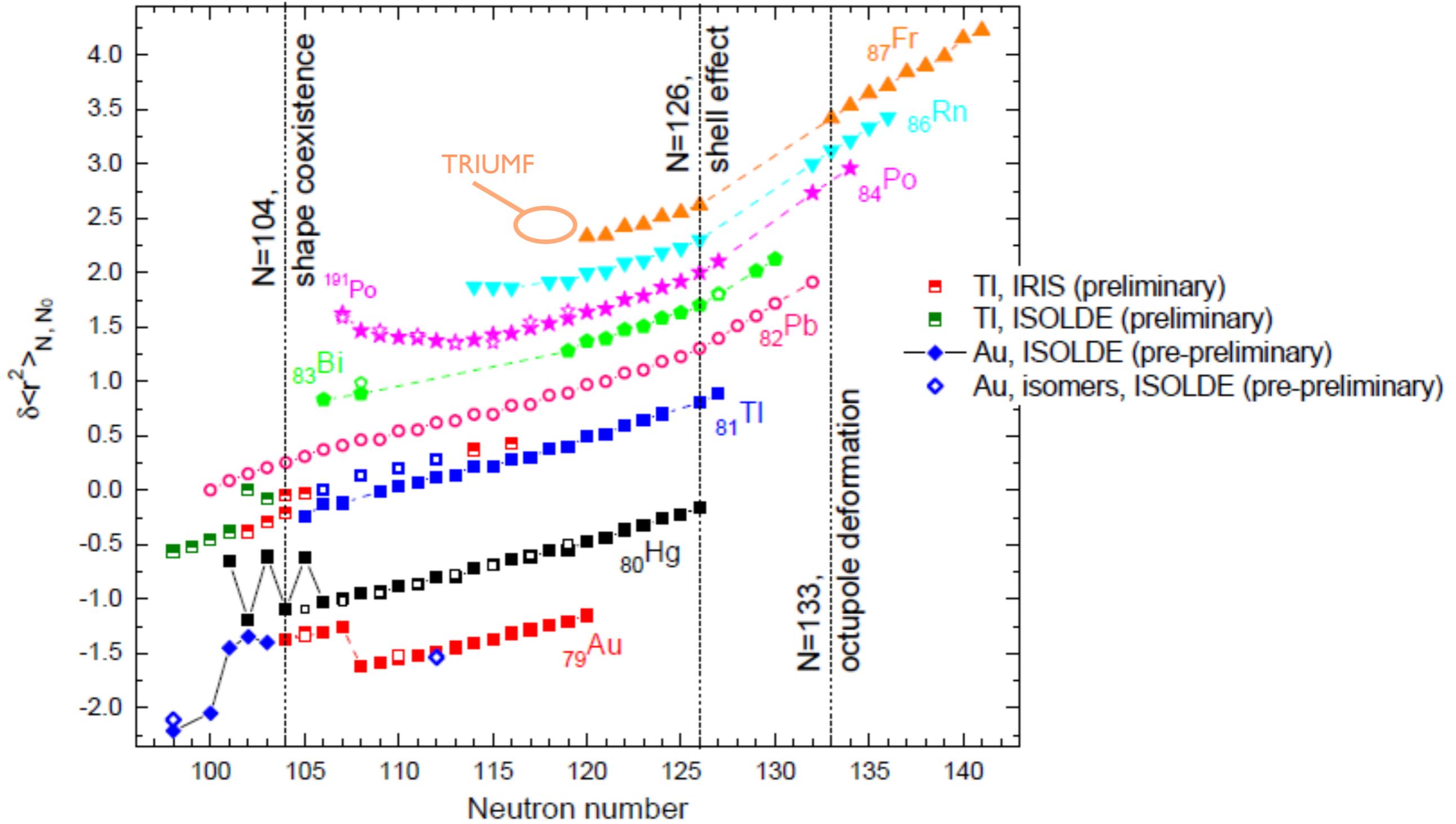
Measurements made at ISOLDE



$6s\ 2S_{1/2} - 6p\ 2P_{1/2}$ (268 nm)

(No quadrupole interaction)

Preliminary data down to Au-177
but further experiments scheduled
(October 2012)



Courtesy Andreyev & Barzakh



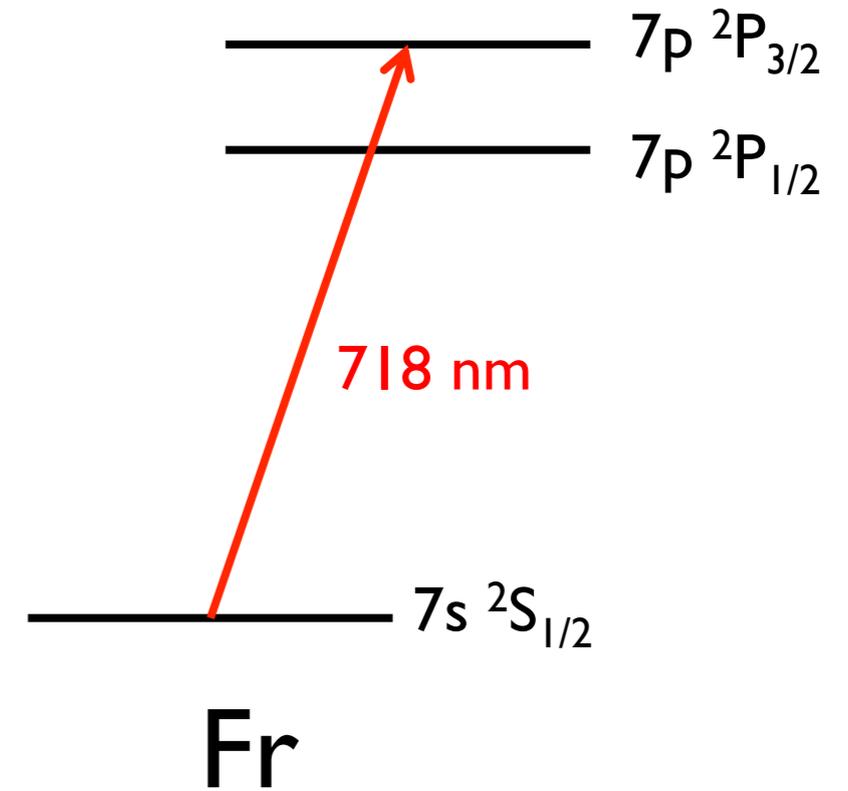
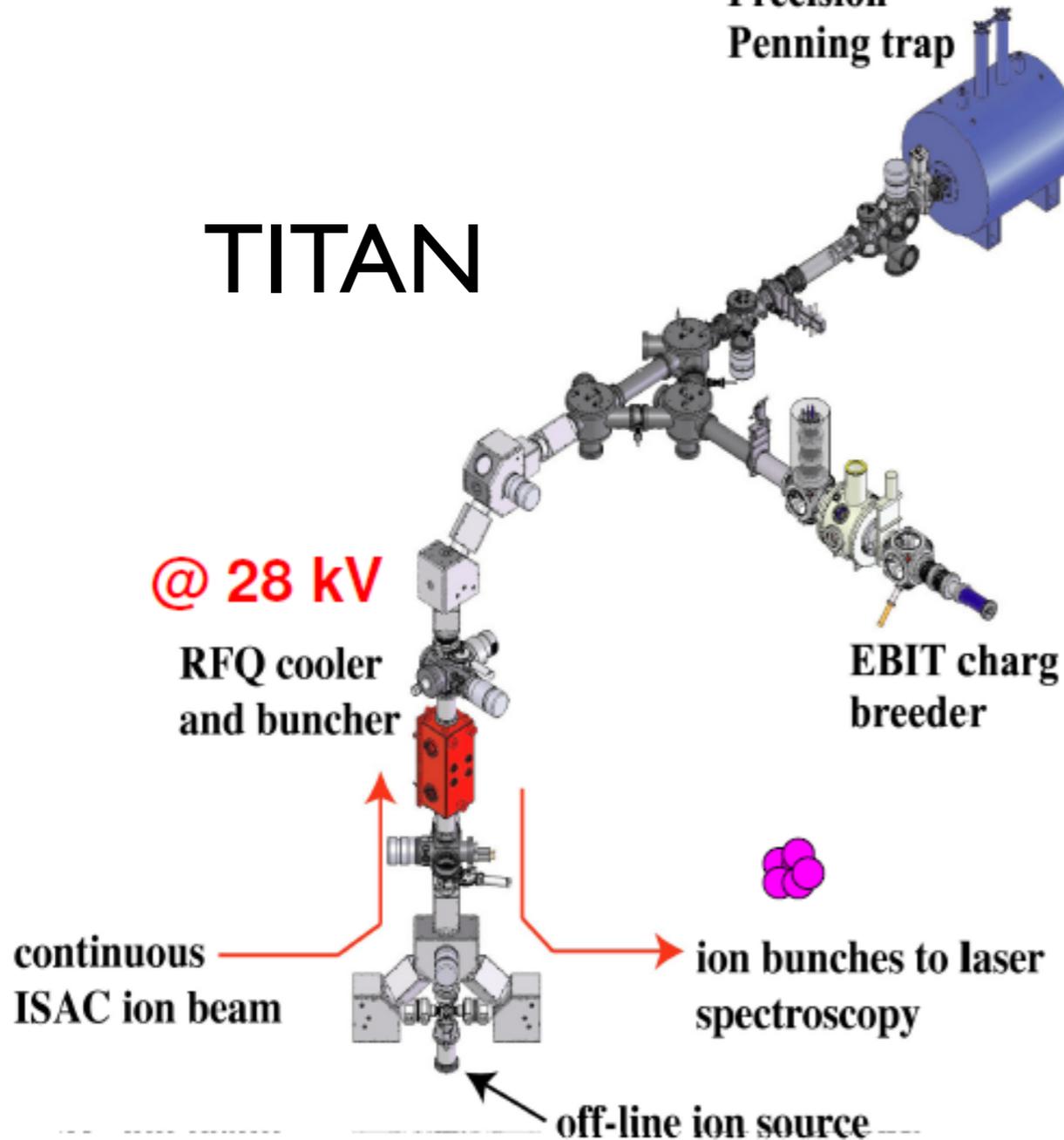
Collinear laser spectroscopy of francium

$A = 205, 206, 206m$

(Annika Voss, PhD Thesis 2012)

TITAN

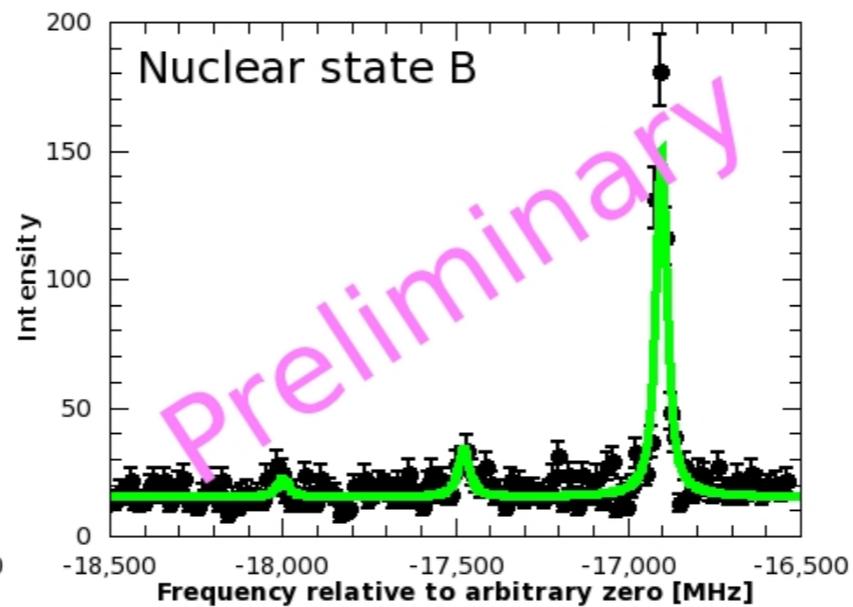
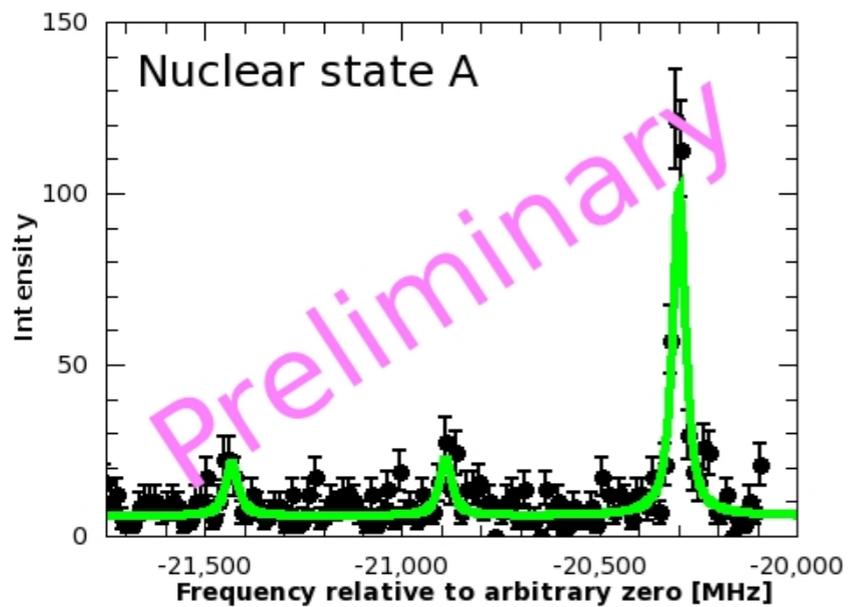
Precision
Penning trap



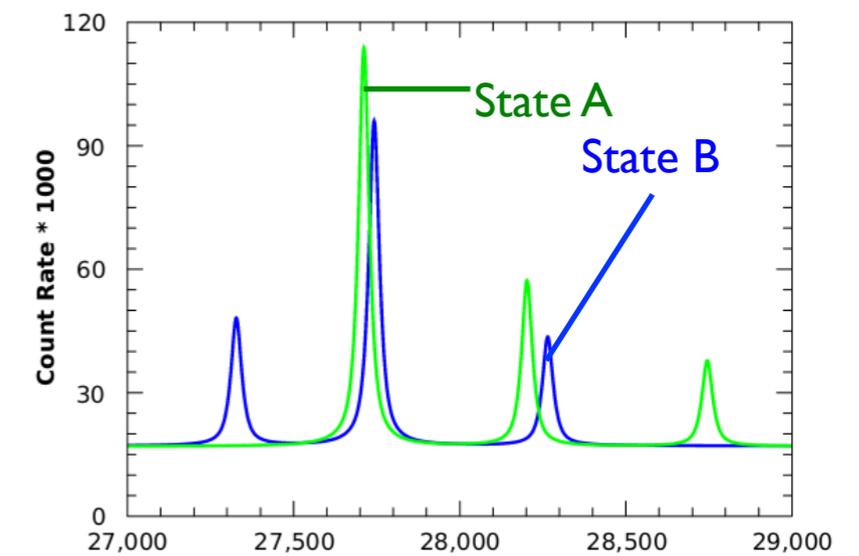
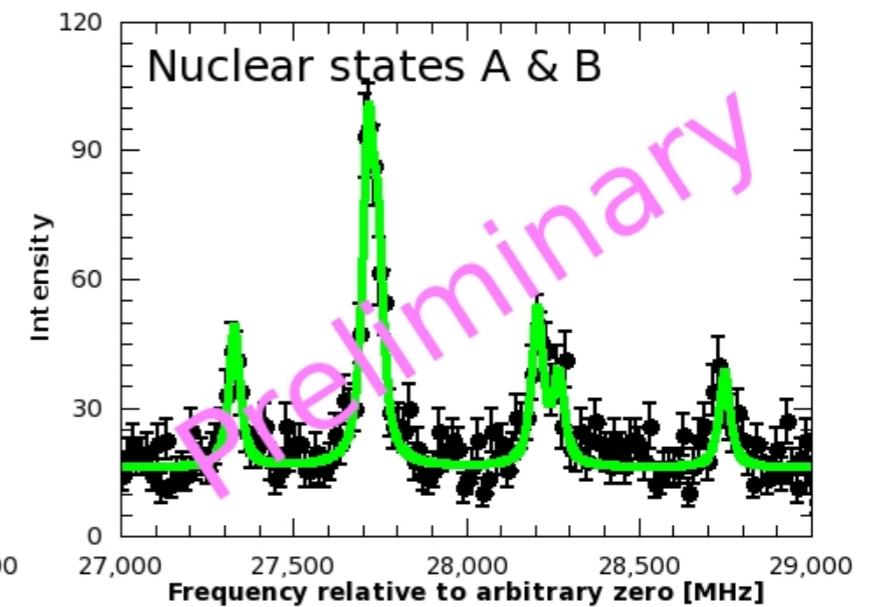
Isotope shifts, μ , Q_s and spins measured.

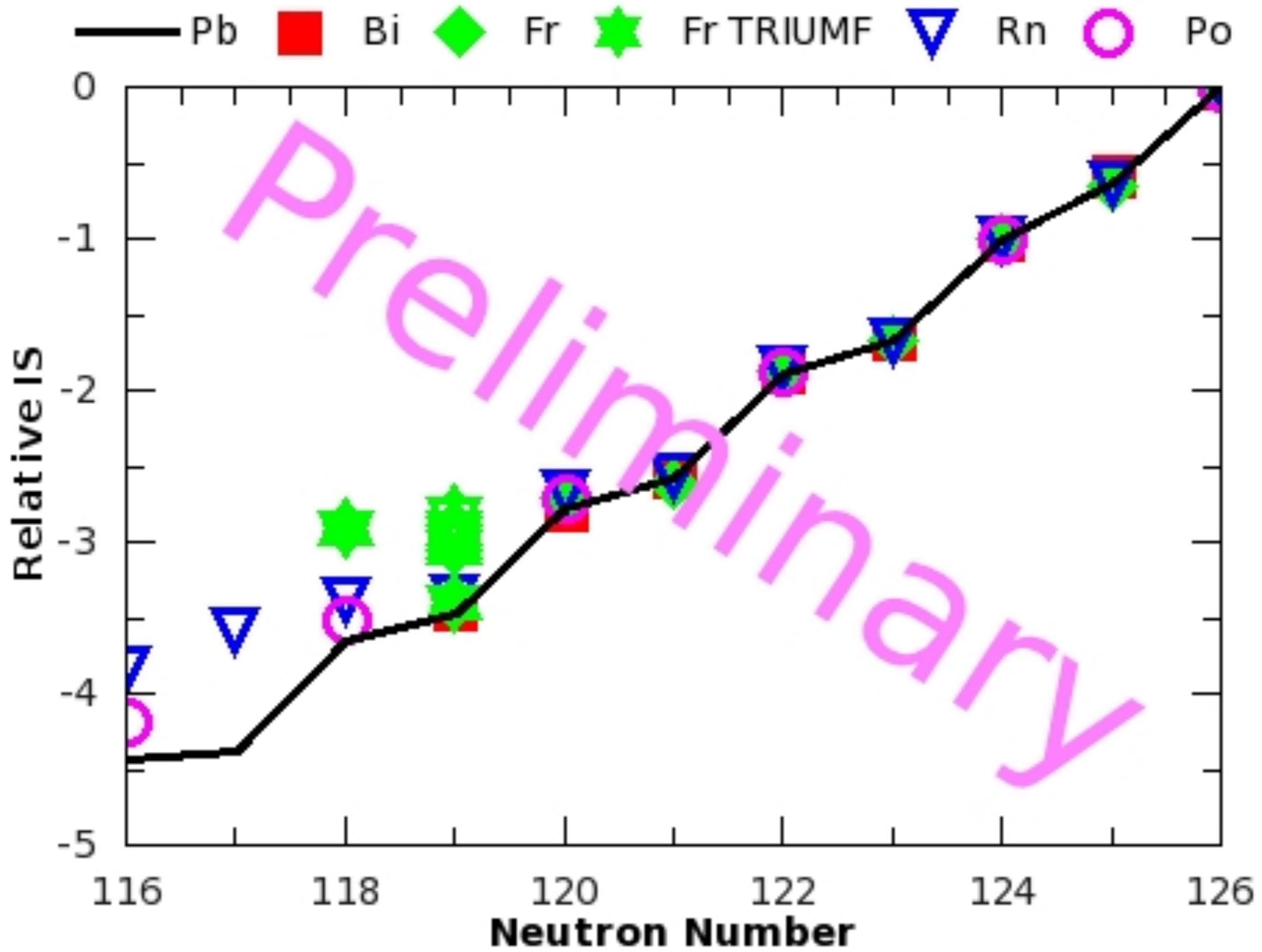
206,206mFr

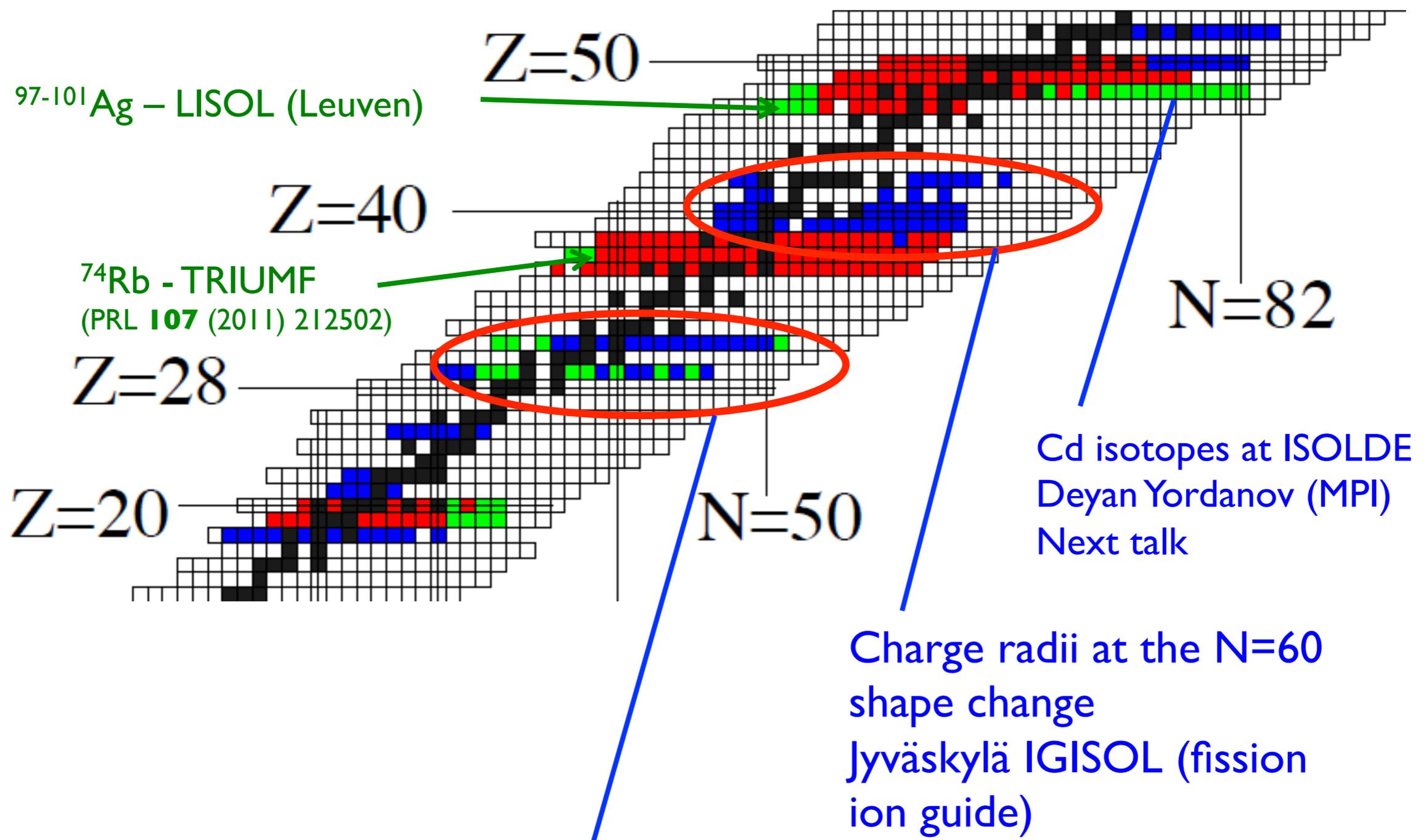
Low frequency multiplets



High frequency multiplets







Moments and radii of Cu and Ga isotopes at ISOLDE

Cd isotopes – Deyan Yordanov

430 nm

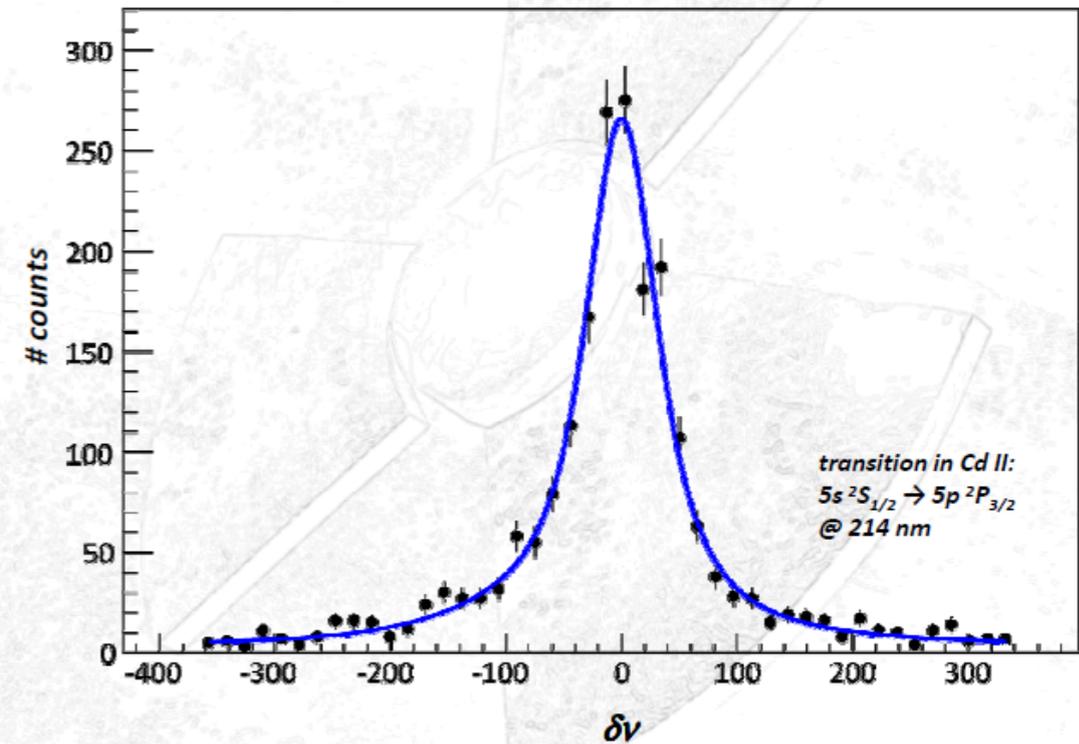
215 nm

860 nm

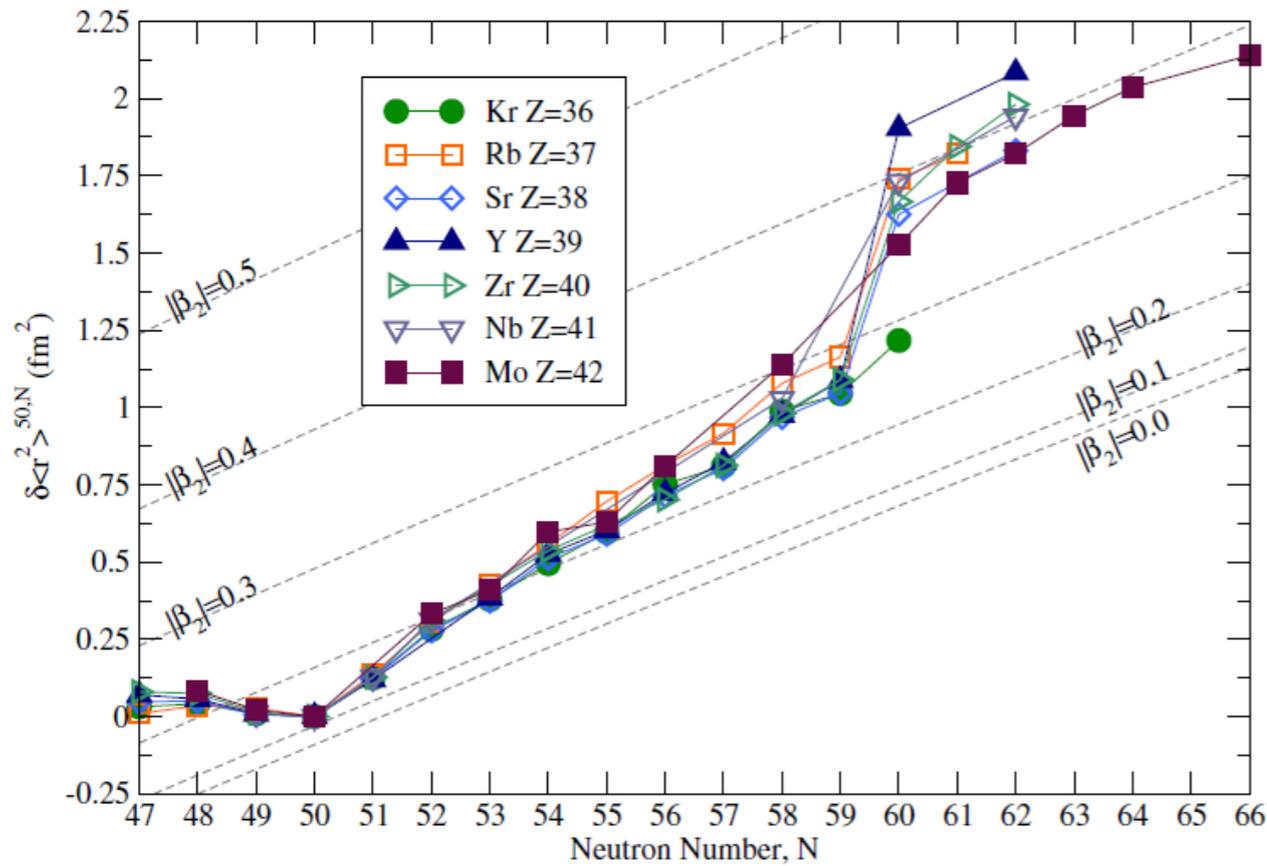
35 mW output maintained over 5 hours

ISOLDE

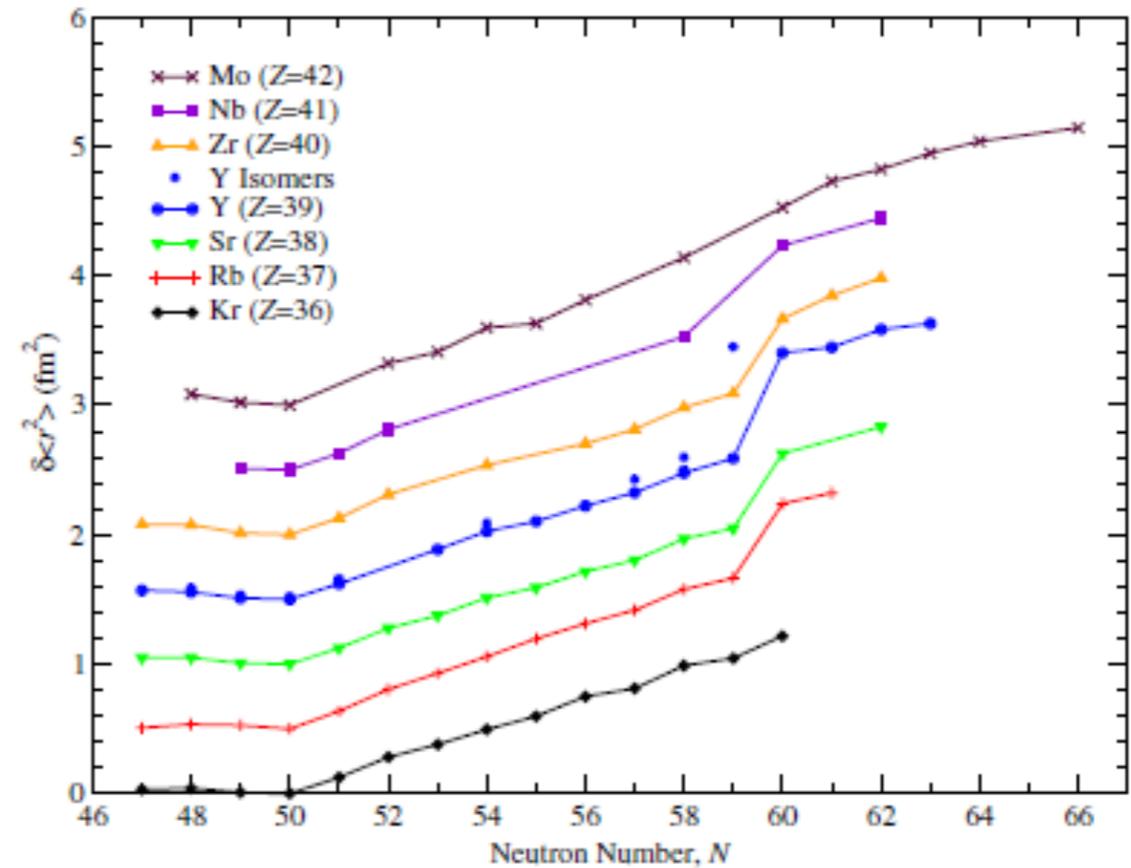
COLLAPS @ ISOLDE / CERN



Charge radii for Kr, Rb, Sr, Y, Zr, Nb and Mo in region of N=60 shape change (Jyväskylä IGISOL)

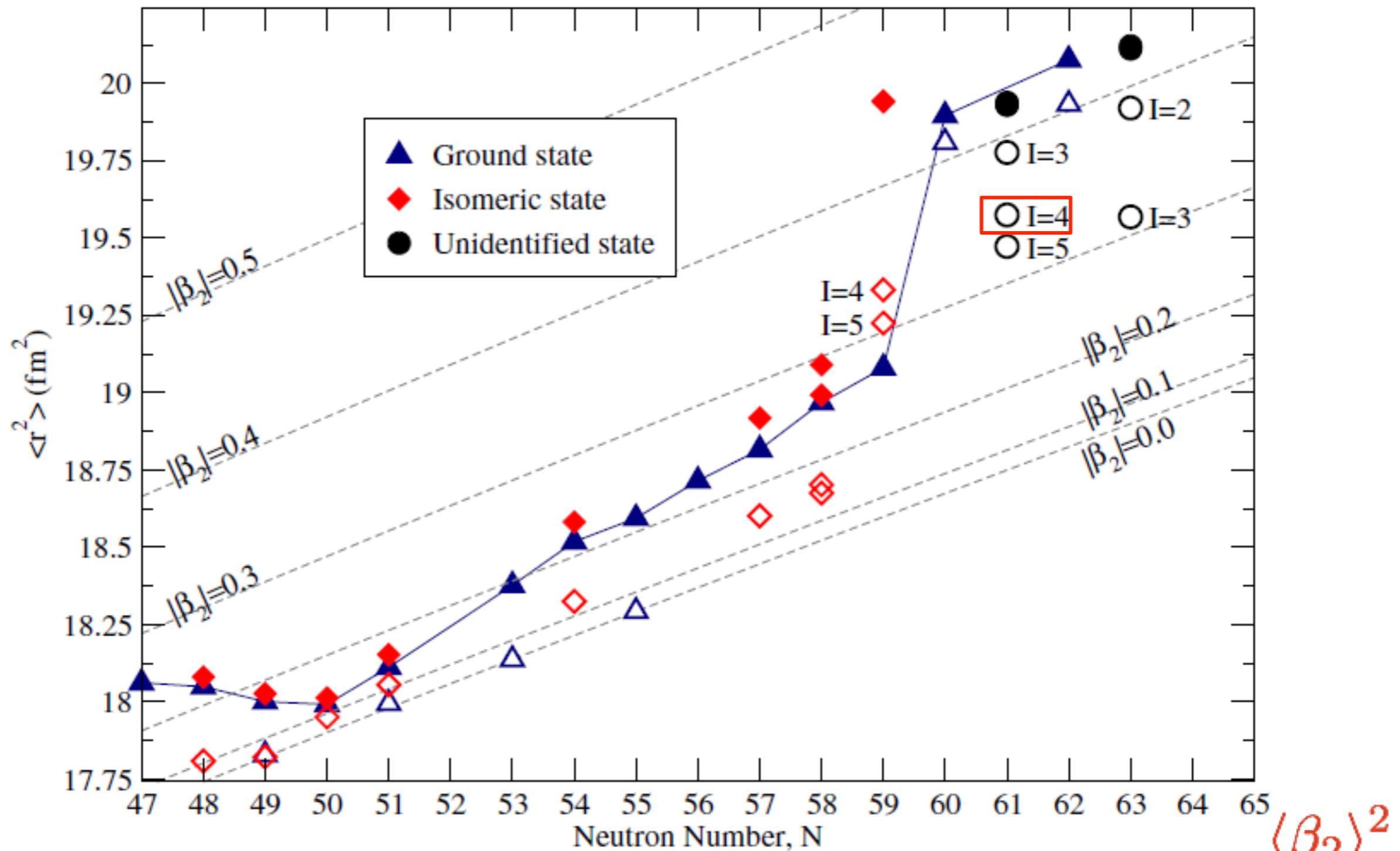


Overlapped



Arbitrarily offset

Droplet model analysis for yttrium isotopes



Open symbols:

static deformation model:

$$\delta \langle r^2 \rangle = \delta \langle r^2 \rangle_{\text{sph}} + \langle r^2 \rangle_{\text{sph}} \frac{5}{4\pi} \delta \langle \beta_2^2 \rangle$$

$\langle \beta_2 \rangle^2$ (with a red arrow pointing to the term)

Motivation for Ga and Cu measurements

Tensor force **attractive** between $l+1/2$ and $l-1/2$
Otsuka et al. Phys. Rev. Lett. **95** (2005) 232502)



- When does $p_{3/2}$ and $f_{5/2}$ ordering invert?
- How good are the new shell model interactions?
(for example, jj44b of Alex Brown, using ^{56}Ni core)

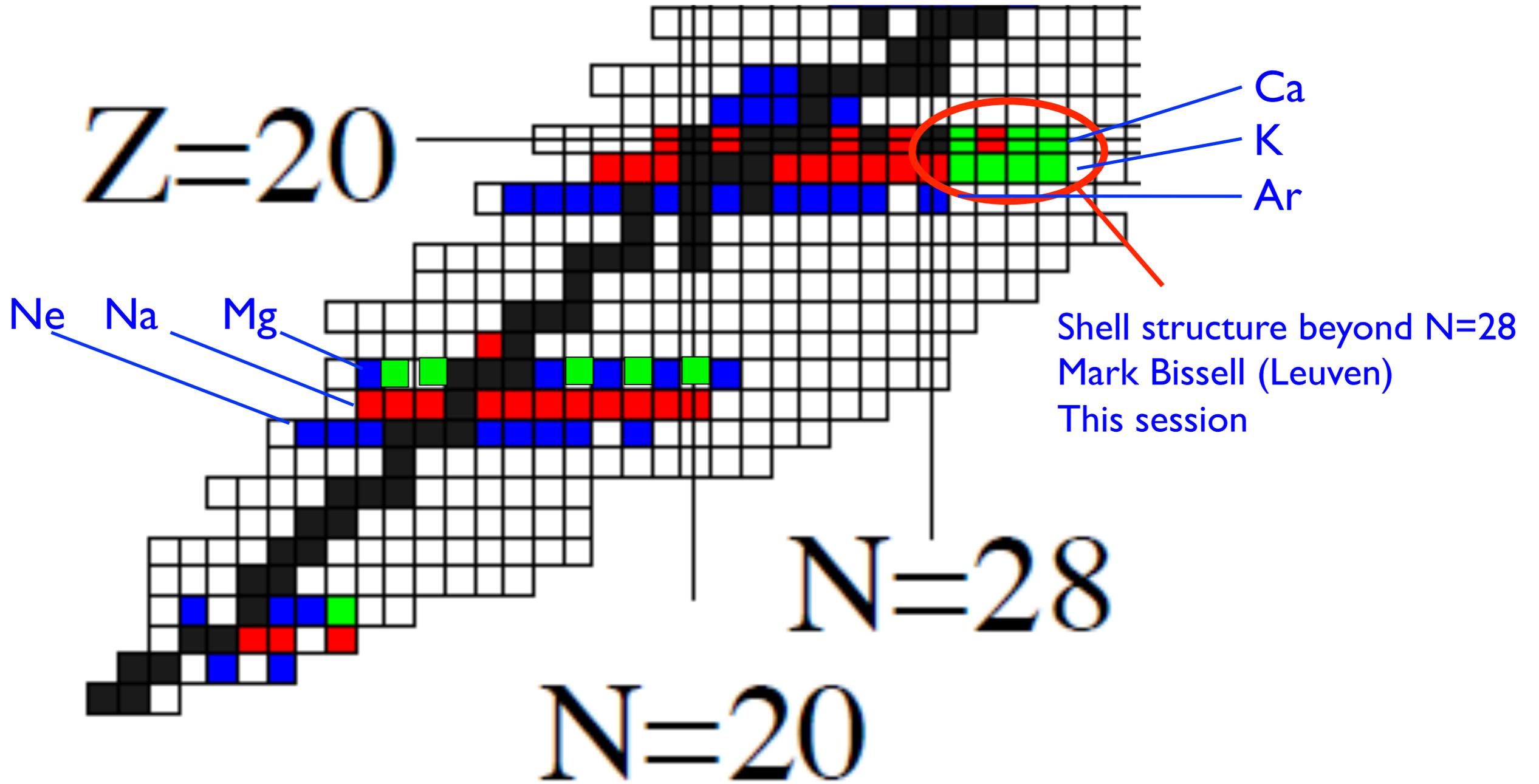
Cu: K.T. Flanagan et al., Phys. Rev. Lett. 103 (2009) 142501

Ga: B. Cheal et al., Phys. Rev. Lett. 104 (2010) 252502

Gallium odd-A spins and moments

A	N	Spin	Magnetic moment		Quadrupole moment	
		I	μ	μ (jj44b)	Q_s	Q_s (jj44b)
63	32	3/2	+1.471(4)	+1.605	+0.210(13)	+0.215
67	36	3/2	+1.848(5)	+2.079	+0.20(2)	+0.117
69	38	3/2	+2.018(4)	+2.284	+0.17(1)	-0.112
71	40	3/2	[+2.256227(2)]	+2.203	+0.106(3)	-0.244
73	42	1/2	+0.209(2)	-0.176	0	0
75	44	3/2	+1.836(4)	+2.441	-0.29(2)	-0.256
77	46	3/2	+2.020(3)	+2.463	-0.21(1)	-0.147
79	48	3/2	+1.047(3)	+2.543	+0.16(1)	-0.057
81	50	5/2	+1.747(5)	+1.477	-0.048(8)	-0.035

Charge radii of light nuclei



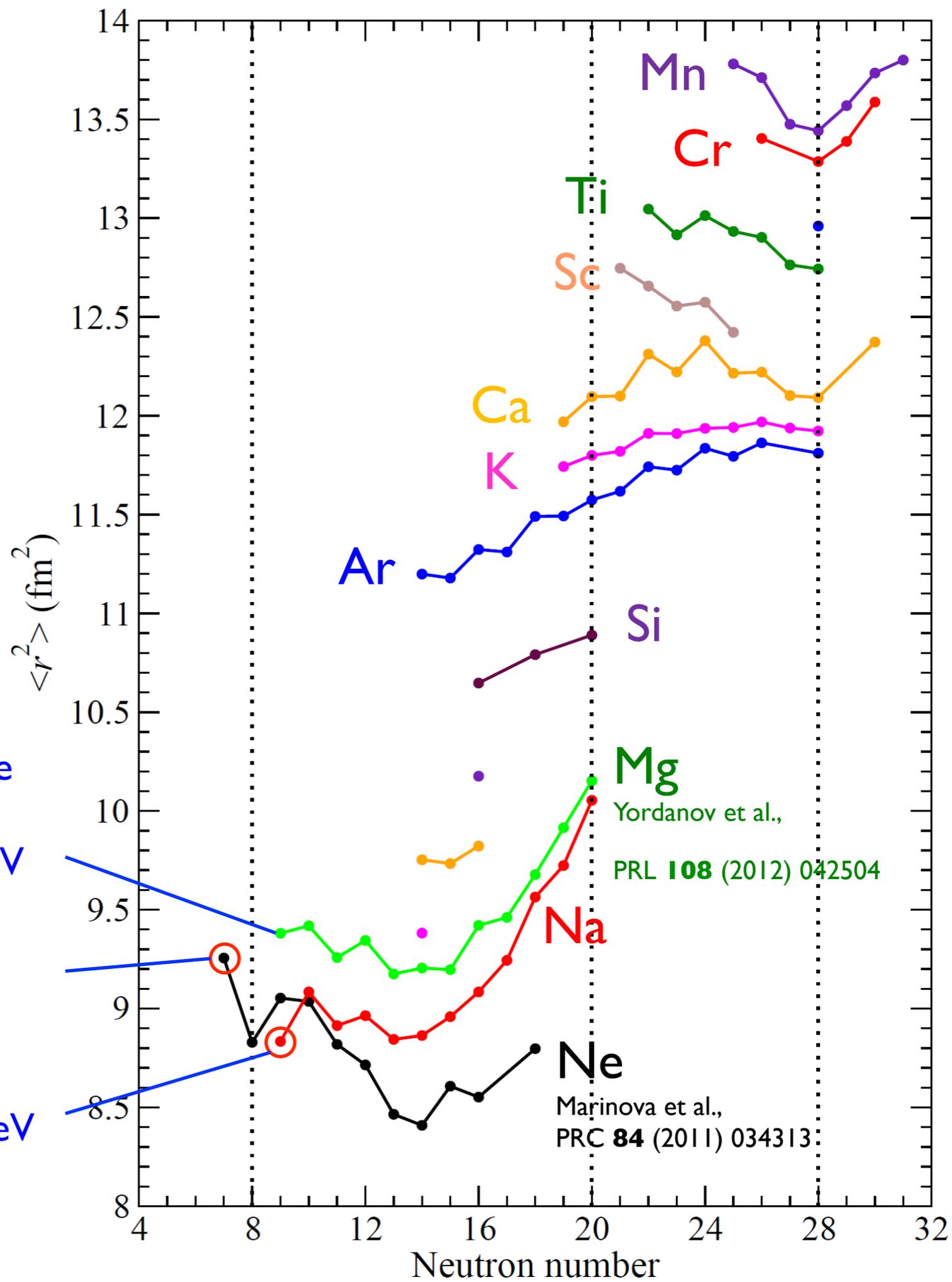
Proton haloes?

○ = Isotope at proton drip line

$S_p = 3.2$ MeV

$S_p = 1.51$ MeV $S_{2p} = 0.93$ MeV

$S_p = 2.19$ MeV



Proton haloes?

Best candidates: ${}^8\text{B}$, ${}^{17}\text{F}$, ${}^{17}\text{Ne}$ (Coulomb barrier in heavier nuclei will inhibit proton tunnelling beyond the nuclear potential)

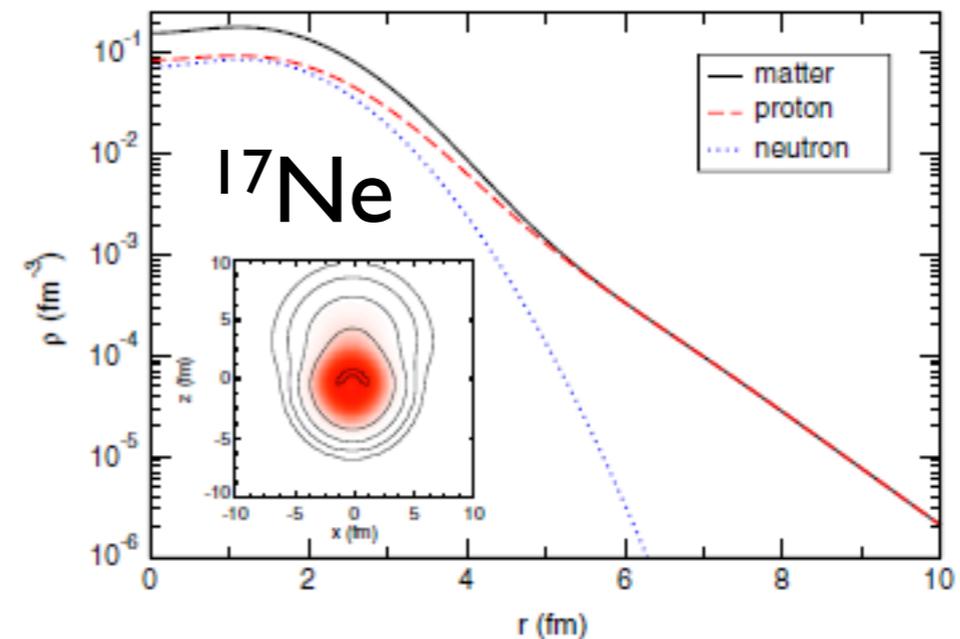
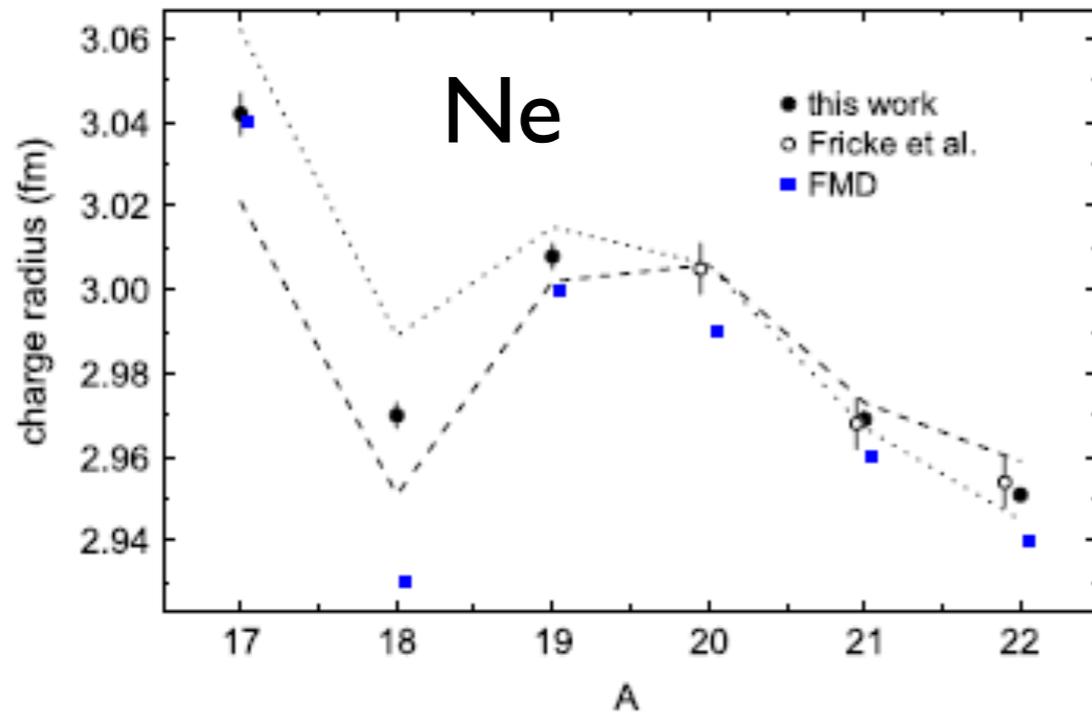
PRL 101, 252502 (2008)

PHYSICAL REVIEW LETTERS

week ending
19 DECEMBER 2008

Masses and Charge Radii of ${}^{17-22}\text{Ne}$ and the Two-Proton-Halo Candidate ${}^{17}\text{Ne}$

W. Geithner,¹ T. Neff,² G. Audi,³ K. Blaum,^{1,2,*} P. Delahaye,⁴ H. Feldmeier,² S. George,^{1,2} C. Guénaut,³ F. Herfurth,² A. Herlert,^{4,5} S. Kappertz,¹ M. Keim,¹ A. Kellerbauer,^{4,*} H.-J. Kluge,^{2,6} M. Kowalska,⁴ P. Lievens,⁷ D. Lunney,³ K. Marinova,⁸ R. Neugart,¹ L. Schweikhard,⁵ S. Wilbert,¹ and C. Yazidjian²

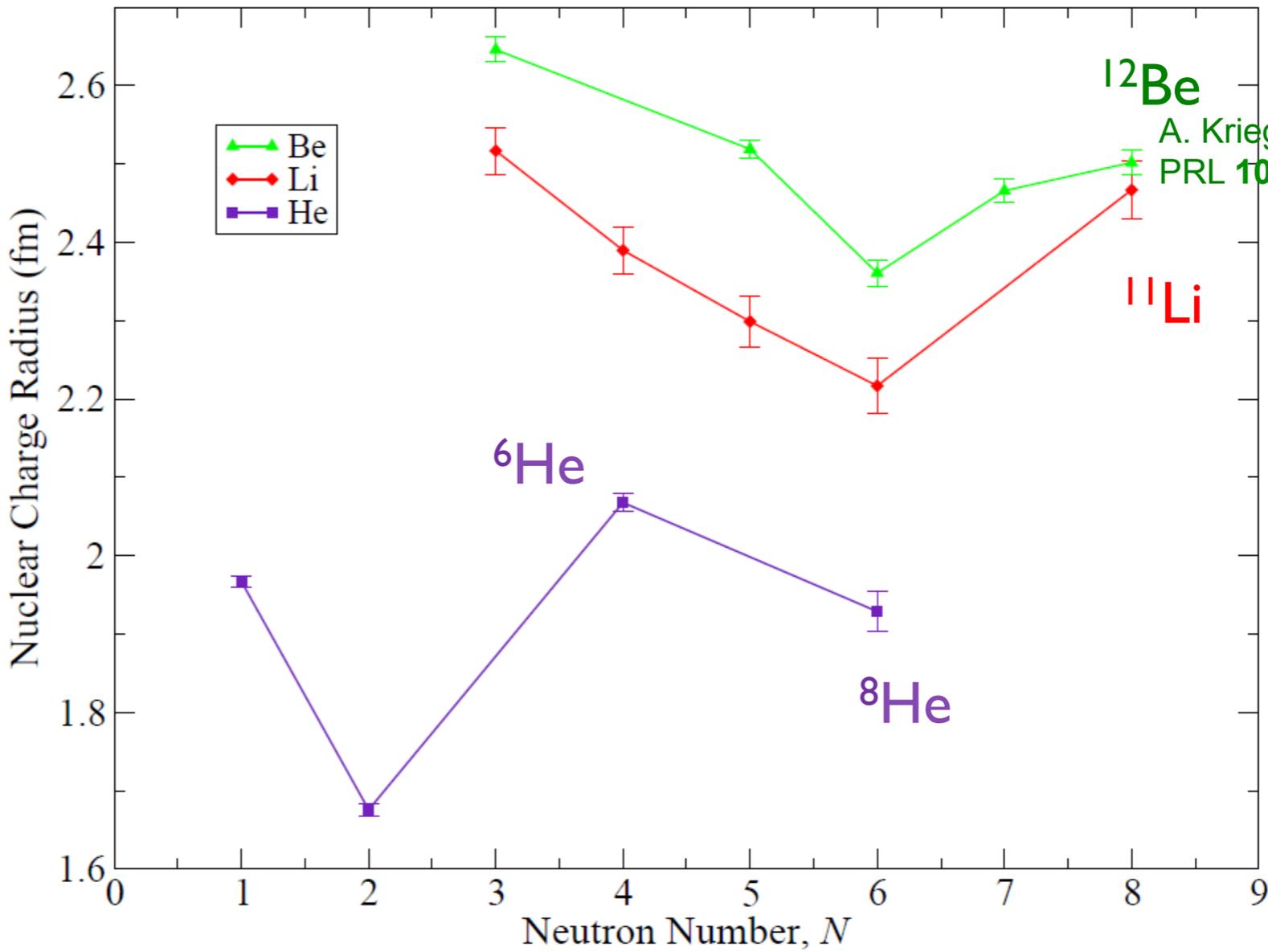


Probability of finding proton at $r > 5$ fm is 40%

Conclusion:

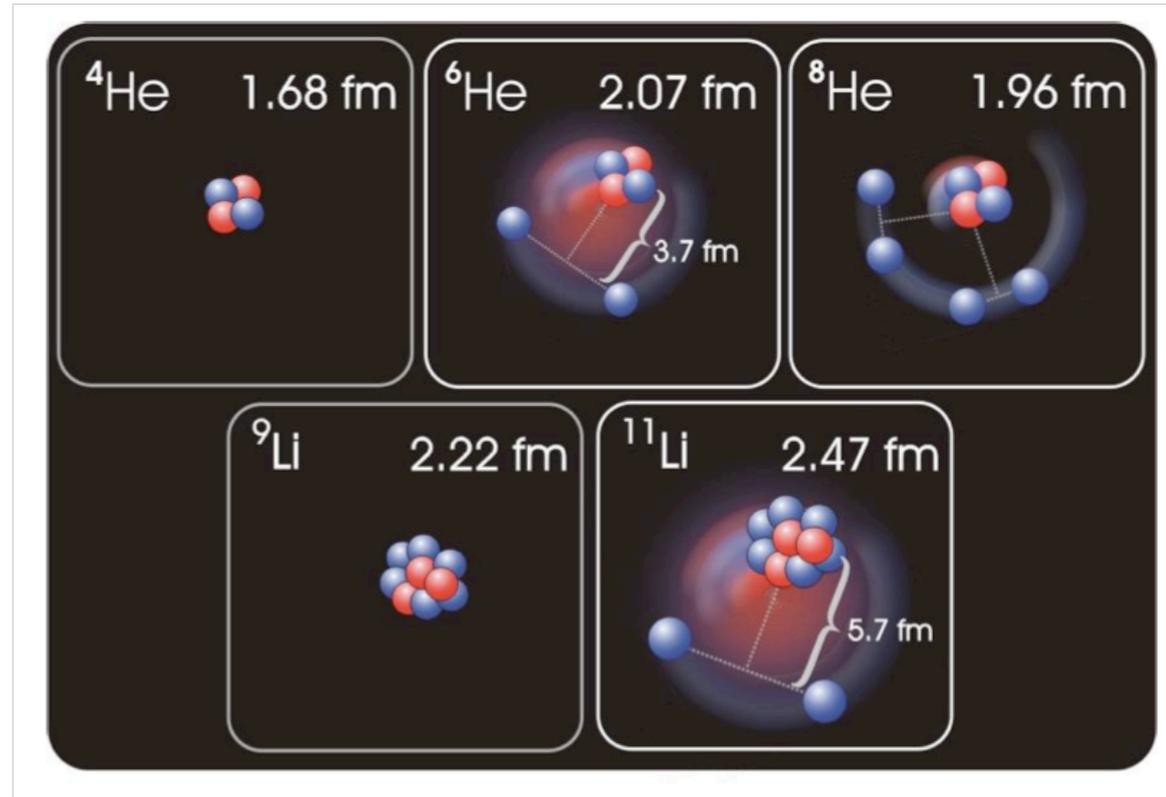
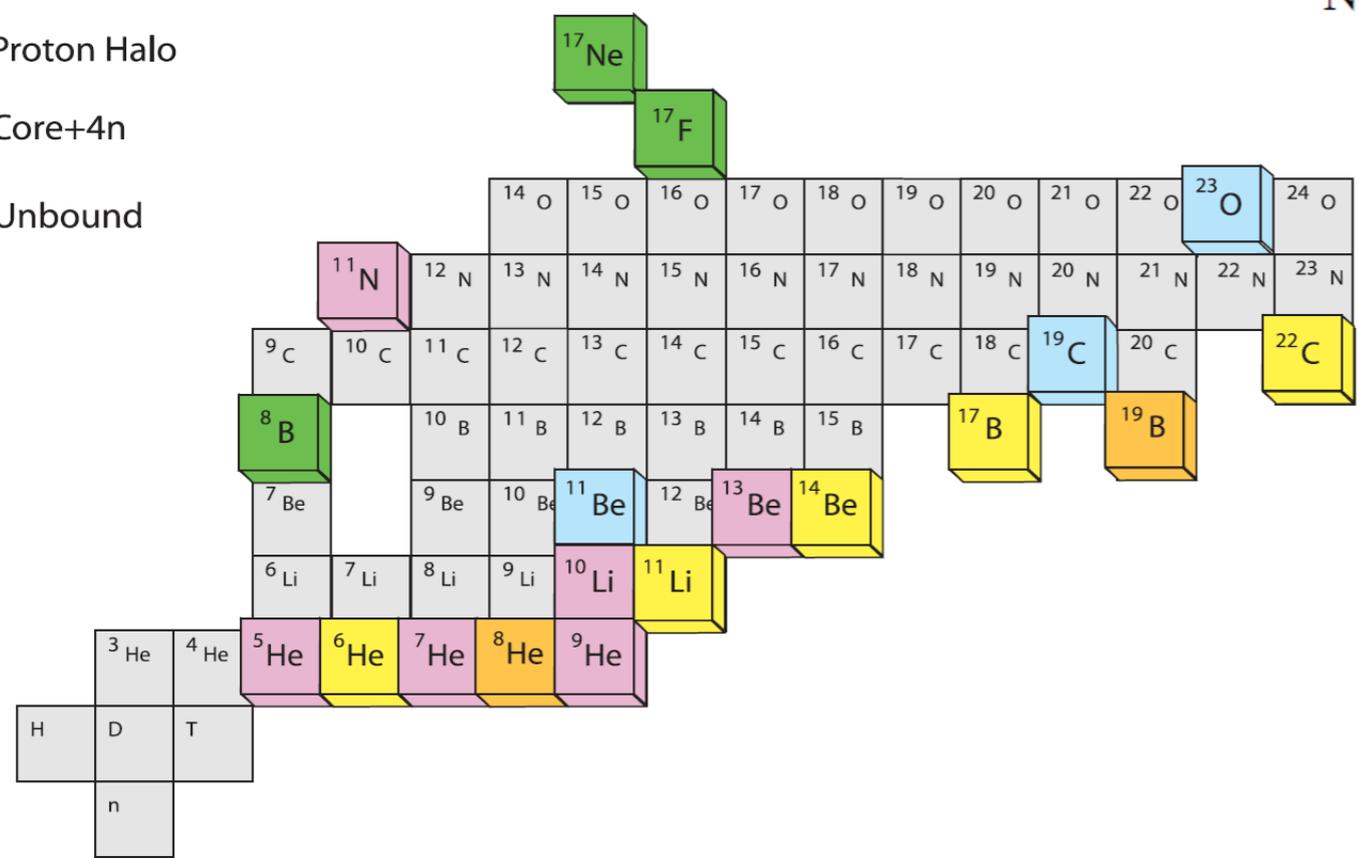
s^2 proton admixture in ${}^{17}\text{Ne}$ ground state is about 40% - development of a proton halo component, but not a well-developed halo.

Cluster structure of light nuclei



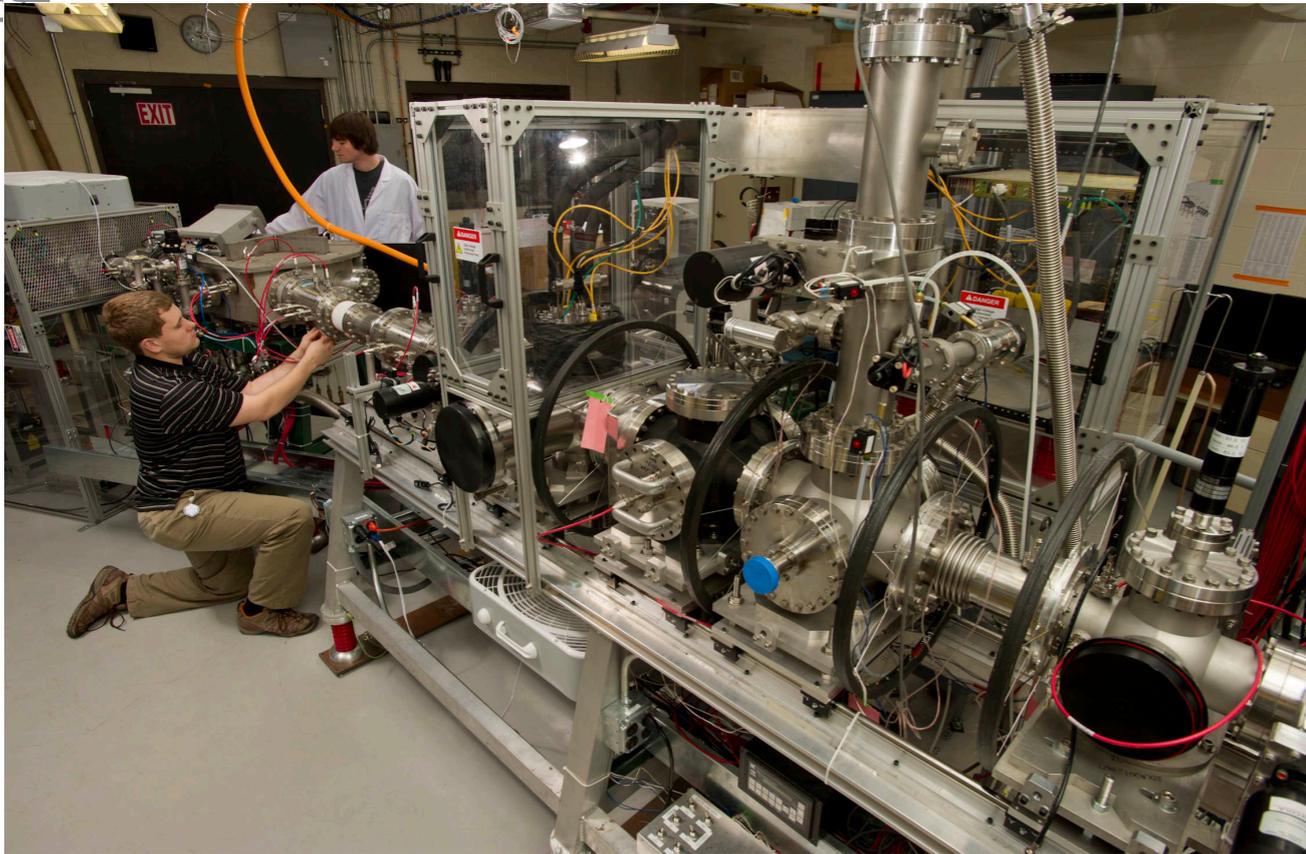
A. Krieger et al.,
PRL **108** (2012)142501

- One-Neutron Halo
- Borromean
- Proton Halo
- Core+4n
- Unbound

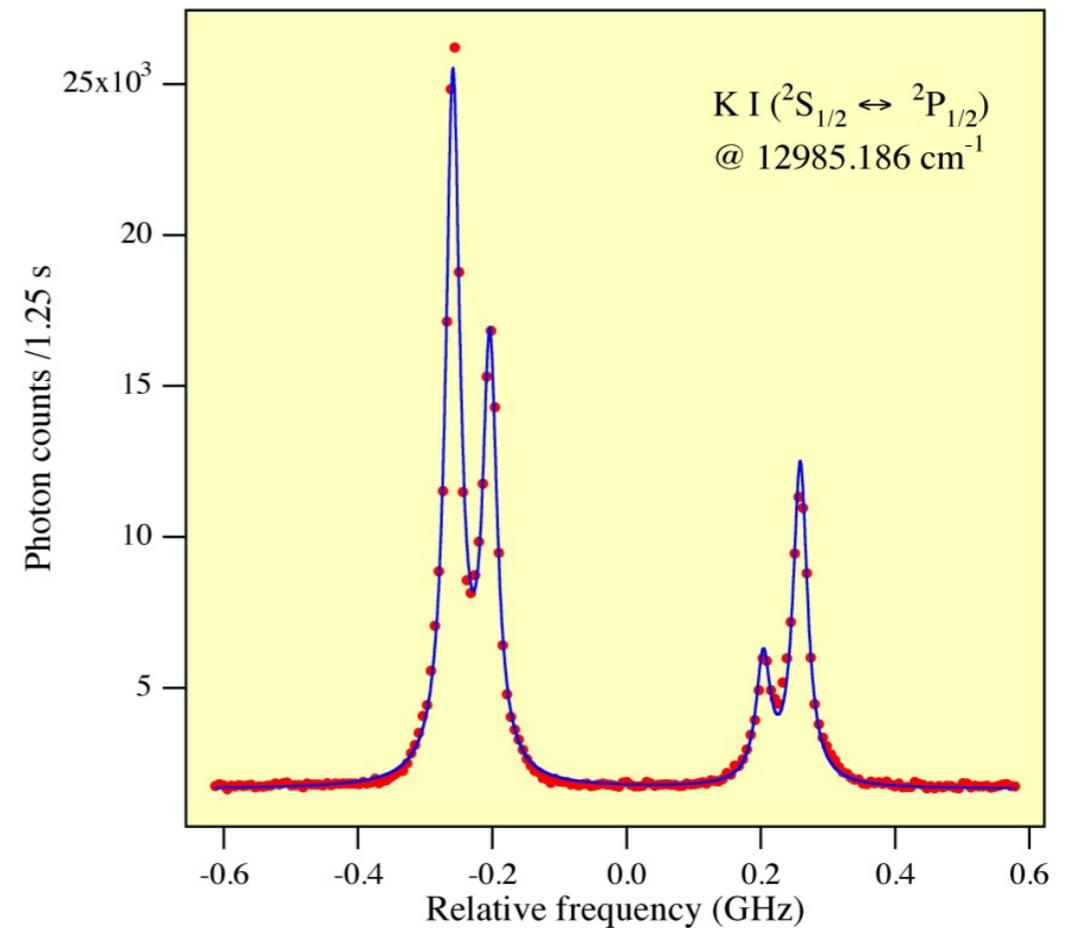


Coming very soon...

BEam COoling and LAser spectroscopy (BECOLA) facility at NSCL



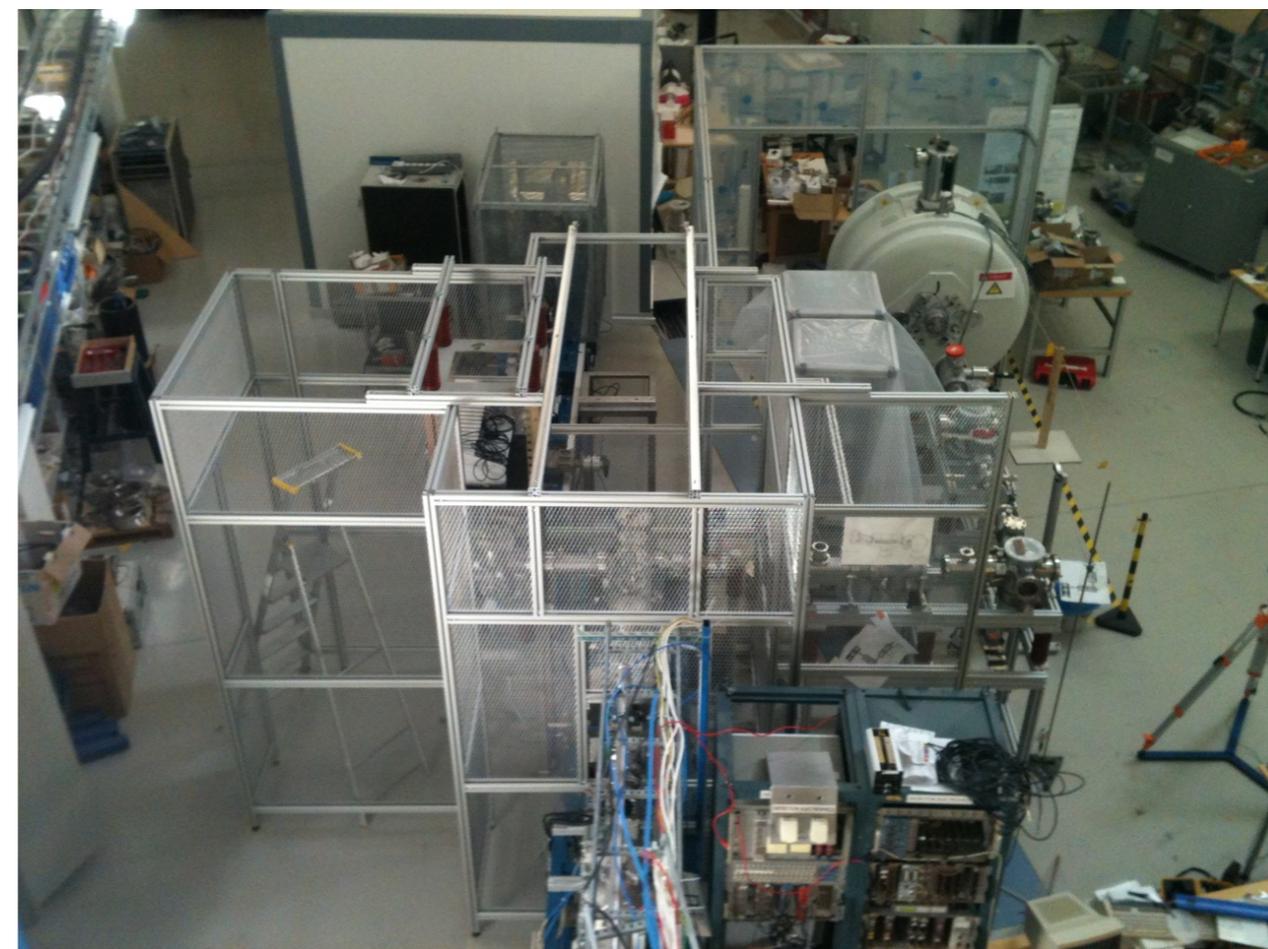
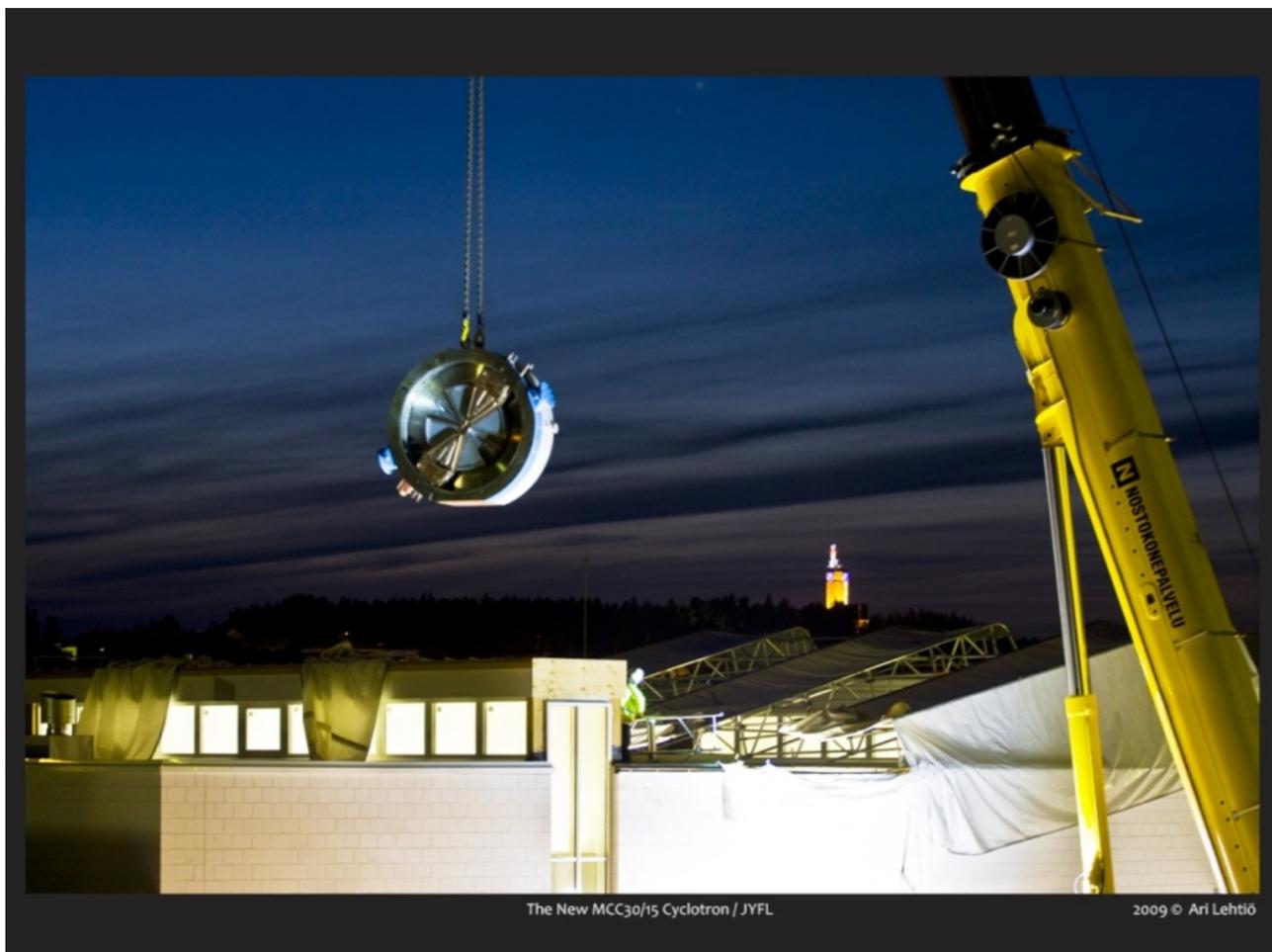
Left: Photograph of the collinear laser beam line of BECOLA.
Below: spectrum of ^{39}K obtained using BECOLA.



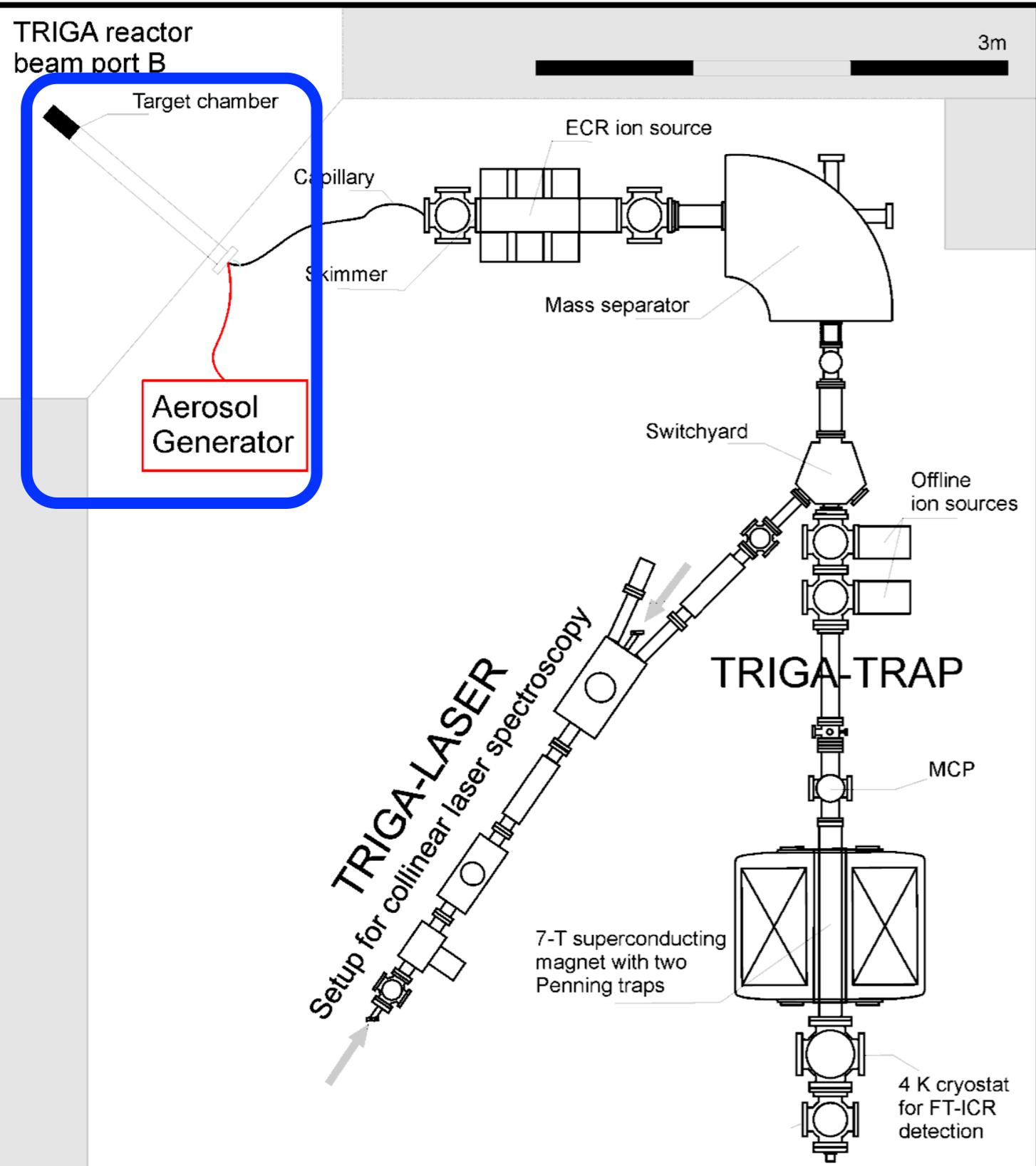
- Commissioning of CLS beam line with stable beams completed
- Cryogenic cooler/buncher under construction and will be completed in 2012
- On-line measurements will commence in 2013 with a NSCL-PAC approved experiment (commissioning run on n-deficient K isotopes)

Poster 34 (A. Klose)
Poster 45 (K. Minamisono)

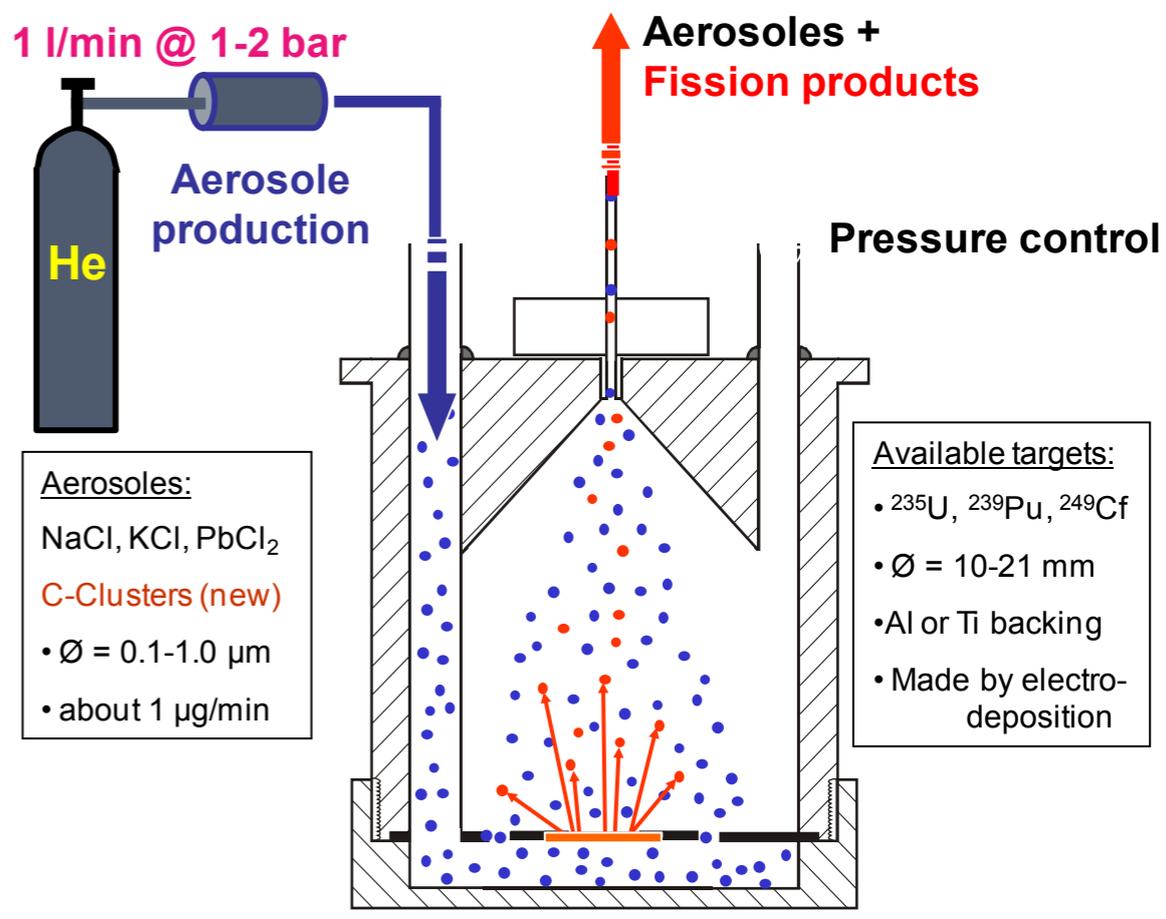
IGISOL IV almost ready at Jyväskylä



TRIGA-Spec (Mainz)



Ion creation



M. Eibach, NIM A 613 (2010) 226–231

Poster 22 (N. Frömmgen)

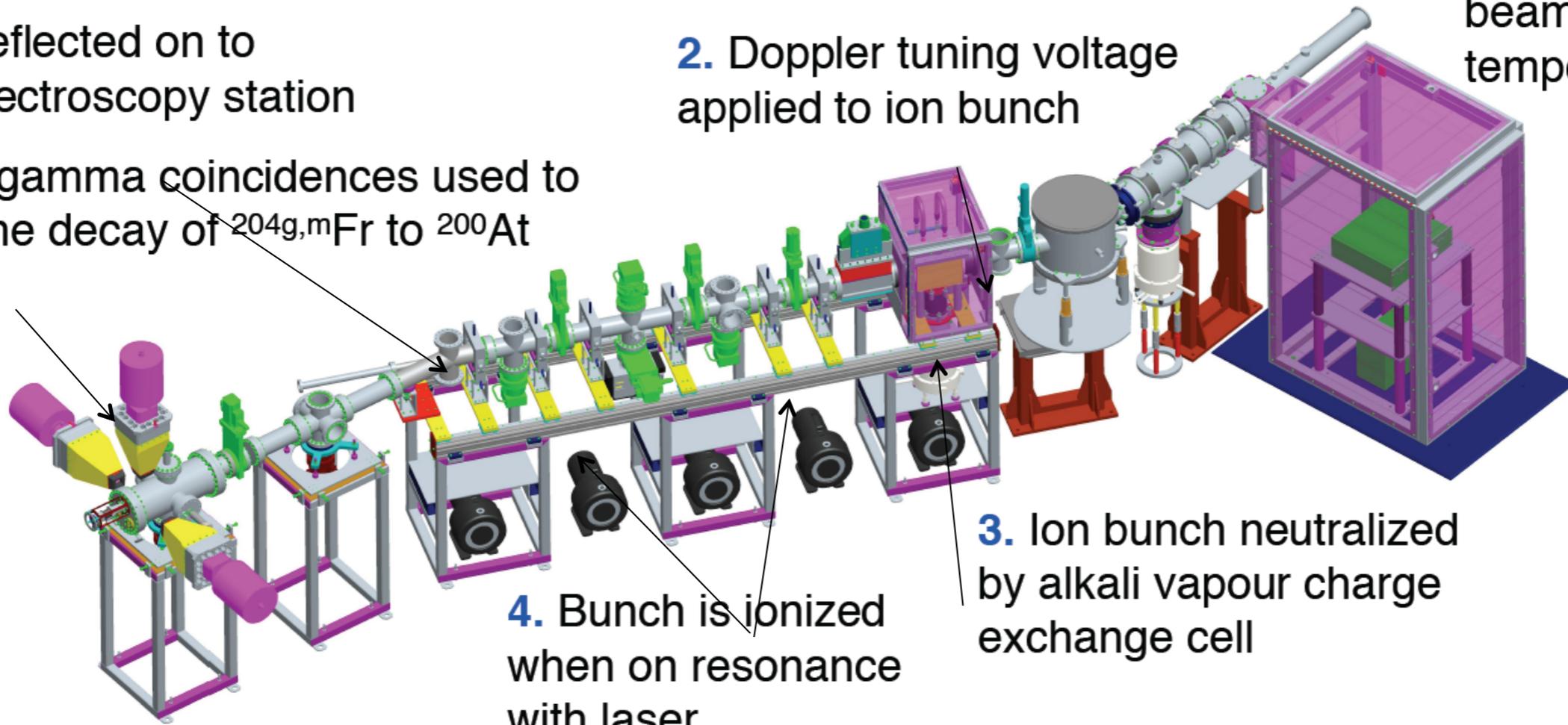
Collinear Resonance Ionisation Spectroscopy CRIS@ISOLDE

5. Ions deflected on to decay spectroscopy station

6. Alpha-gamma coincidences used to identify the decay of $^{204g,m}\text{Fr}$ to ^{200}At

2. Doppler tuning voltage applied to ion bunch

1. Bunched ion beam of $\sim 1\mu\text{s}$ temporal width



4. Bunch is ionized when on resonance with laser
(two-step resonance ionisation)

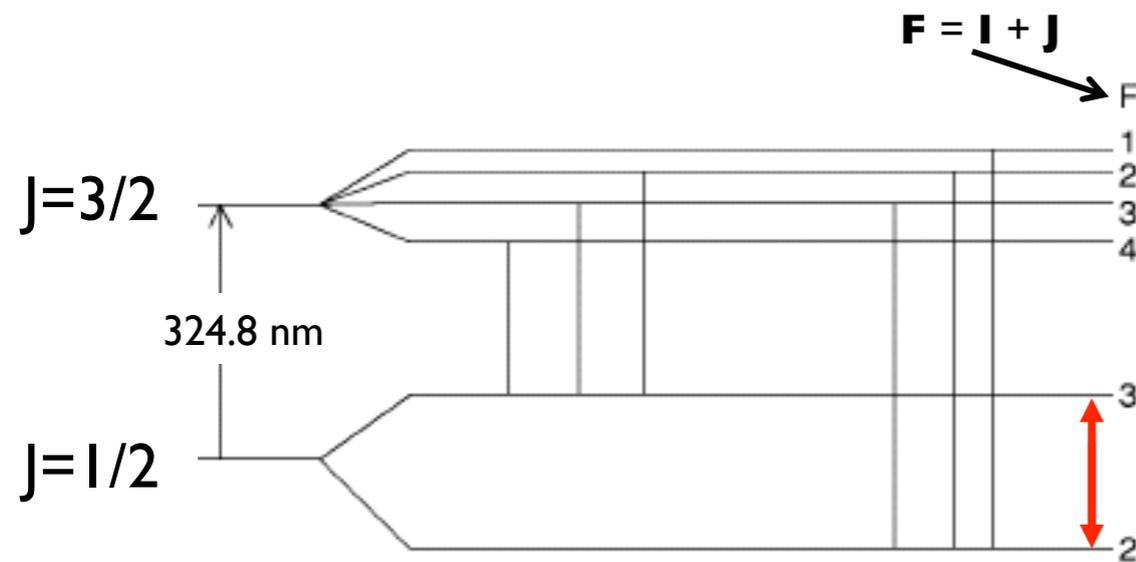
3. Ion bunch neutralized by alkali vapour charge exchange cell

Poster 60 (M.M. Rajabali)

Summary

- Recent measurements have concentrated on the most exotic nuclei accessible.
- These data provide stringent tests of nuclear models (shell model interactions, shell structure, FDM in light nuclei).
- The field has been re-invigorated through use of ion beam coolers and in-source RIS techniques.
- Many new facilities and experiments in the pipeline

Determining the nuclear spin, I

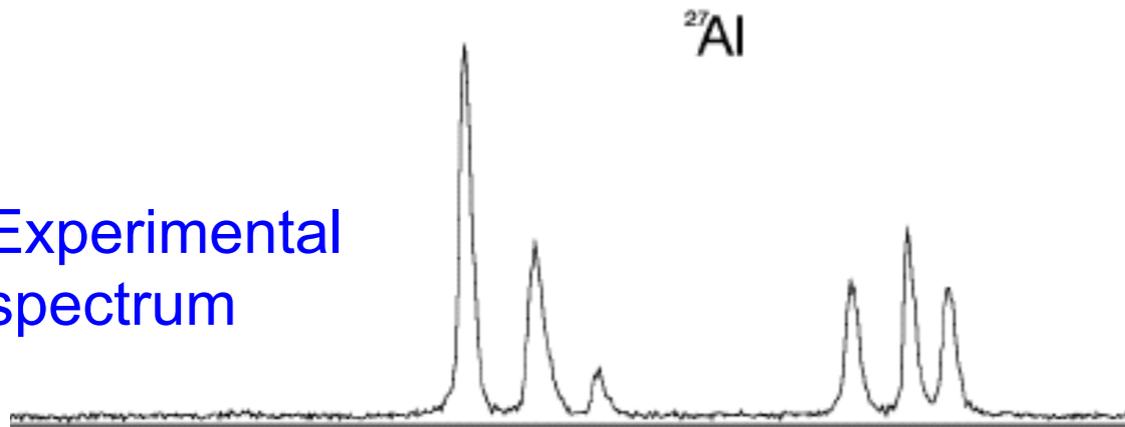


Intervals depend on A_{upper} , B_{upper} , and I , J , F

Interval depends on A_{lower} , and I , J , F

Ratio $A_{\text{upper}}/A_{\text{lower}}$ is independent of nuclear moment (ie same for all isotopes)

Experimental
spectrum

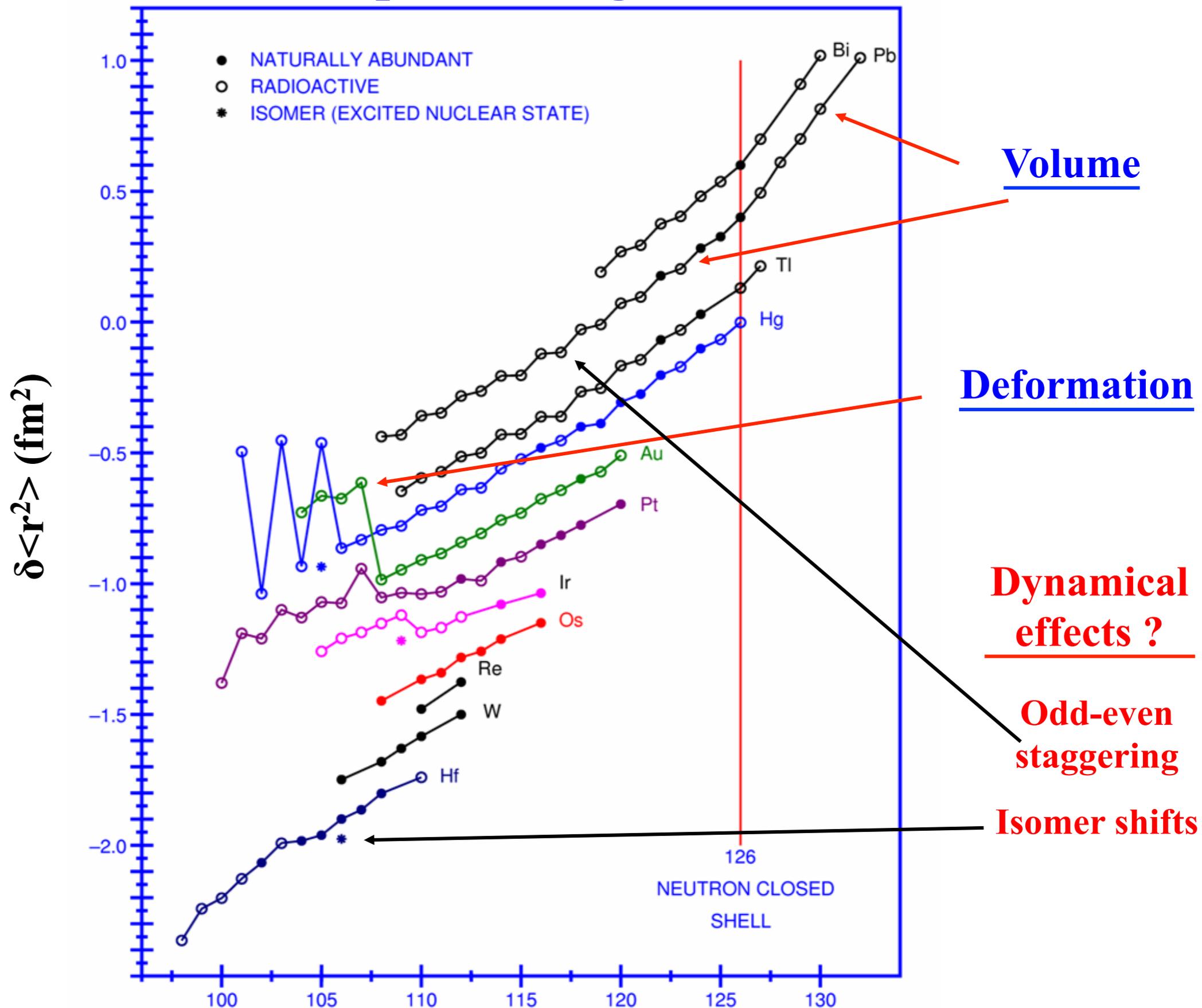


If the **wrong** value of I is used to fit the hyperfine structure then:

- May be impossible to fit structure (position or number of peaks)
- Deduced ratio $A_{\text{upper}}/A_{\text{lower}}$ is wrong
- Deduced relative peak intensities are wrong (Racah coefficients)

Without a definite spin, none of the other nuclear parameters can be deduced

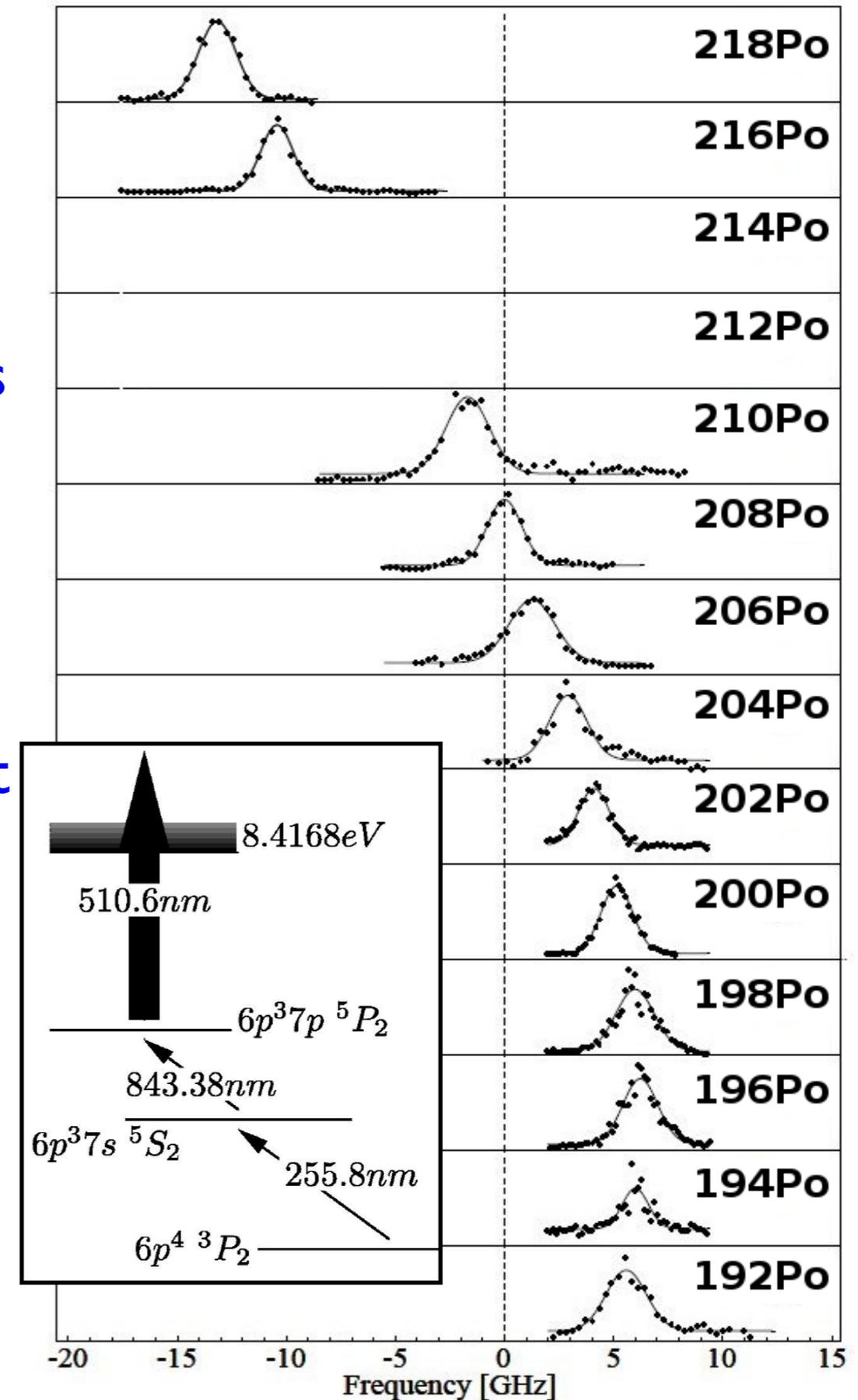
Mean square charge radii



Neutron-deficient Po isotopes

(Cocolios et al, Phys. Rev. Lett. 106 (2011) 052503)

- ISOLDE in-source RIS. Measurements made on the 843nm transition.
- Even-A results published.
- Odd-A hyperfine structures were not fully resolved and further experiments are scheduled (September 2012) using RILIS in narrow band mode and the LIST (laser ion source and trap) method



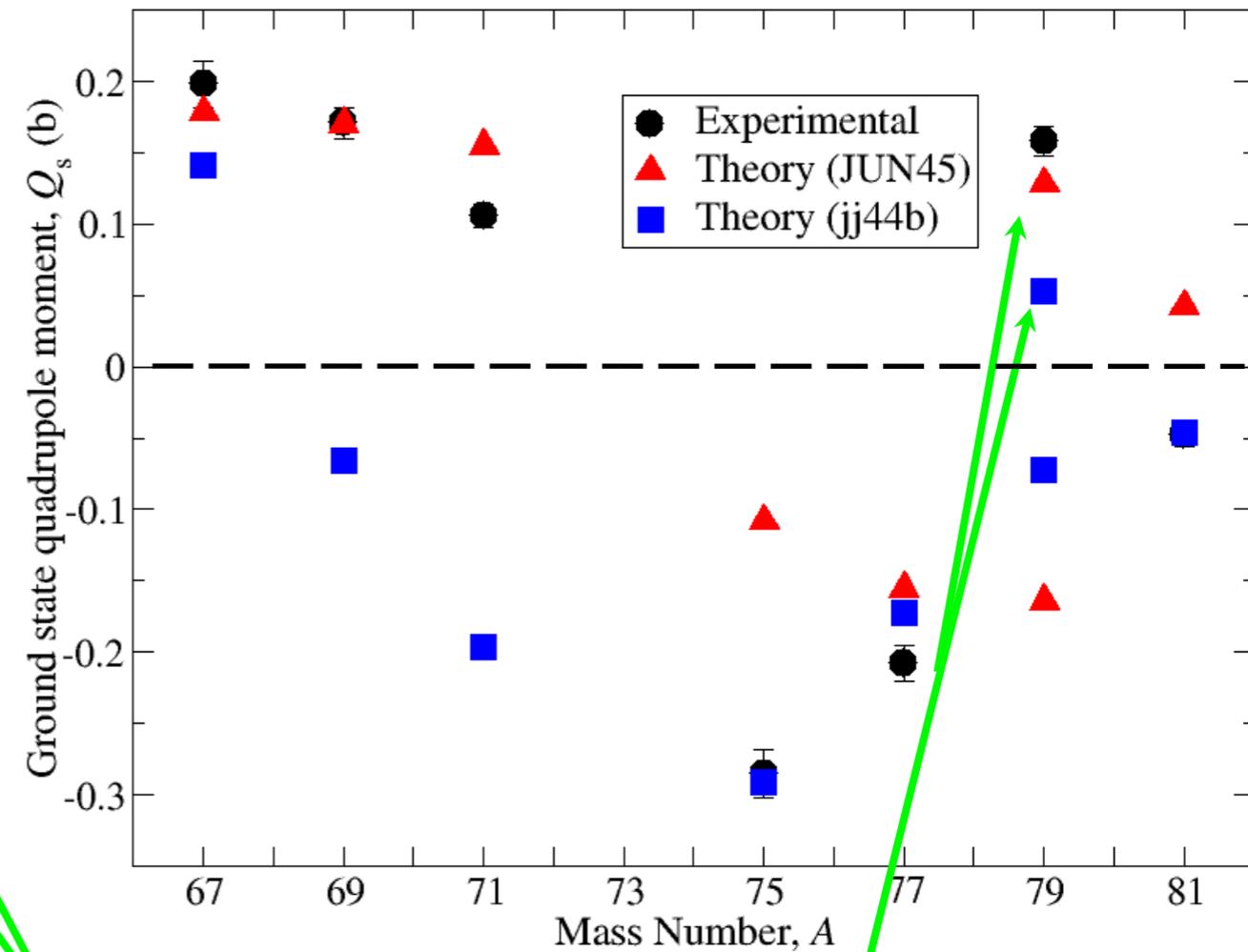
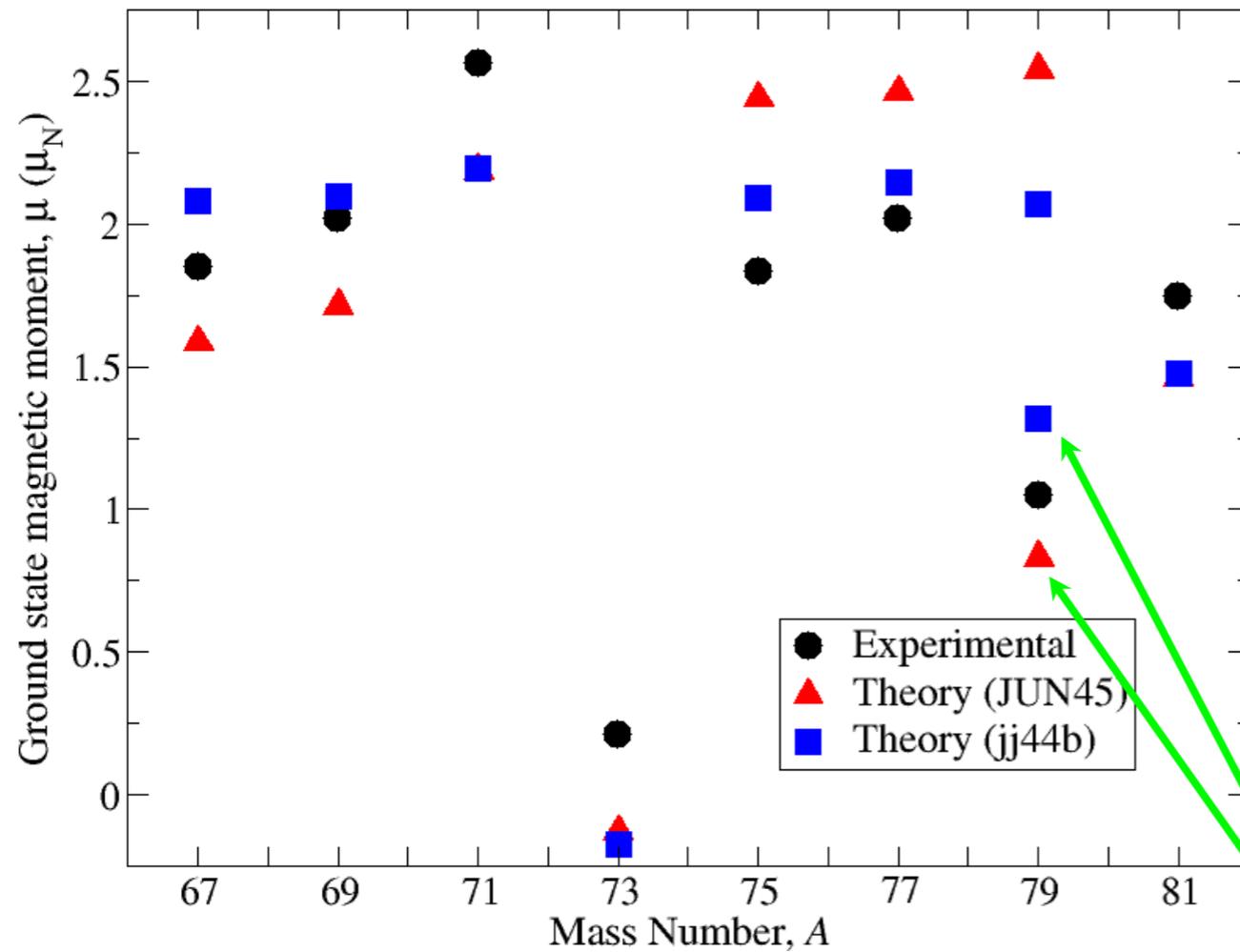
Ga shell model calculations (^{56}Ni core)

JUN45 (Honma et al)

jj44b (Alex Brown)

Magnetic dipole

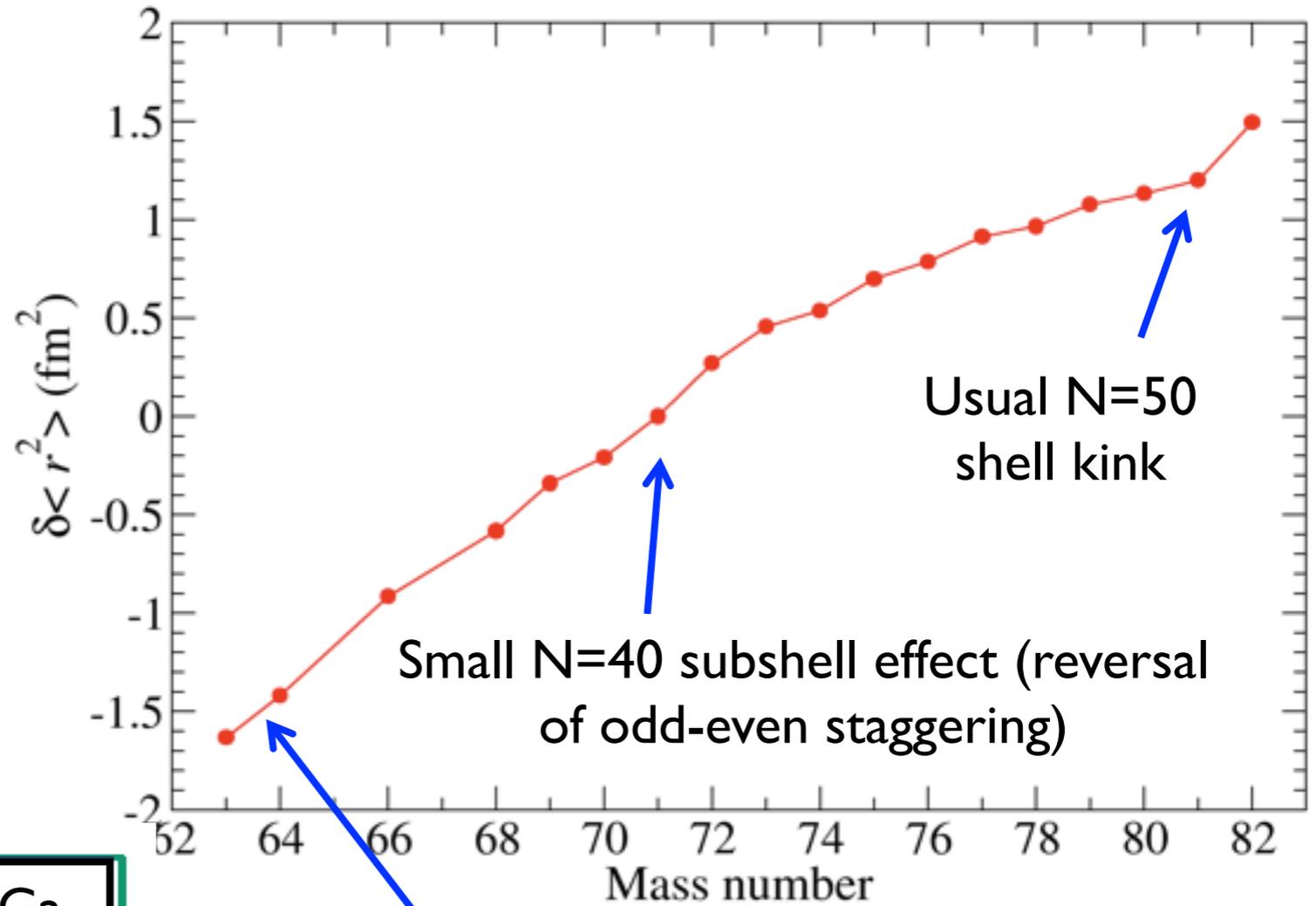
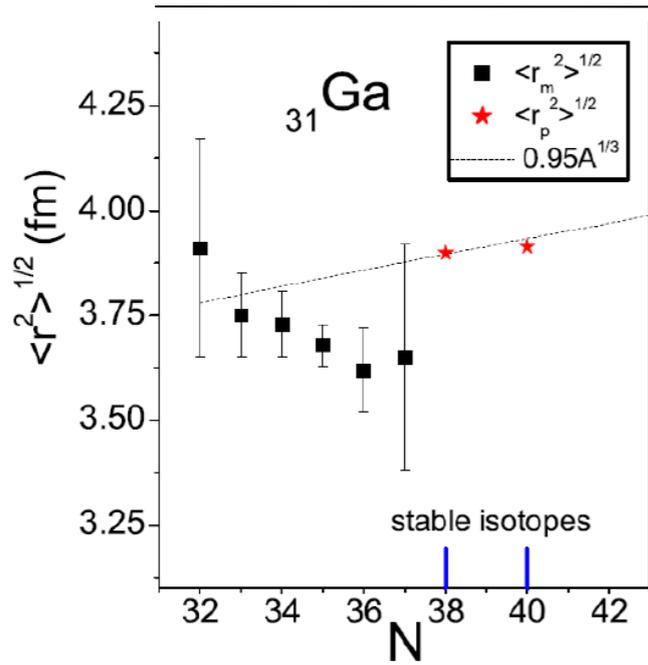
Electric quadrupole



Predictions for **second 3/2 states**

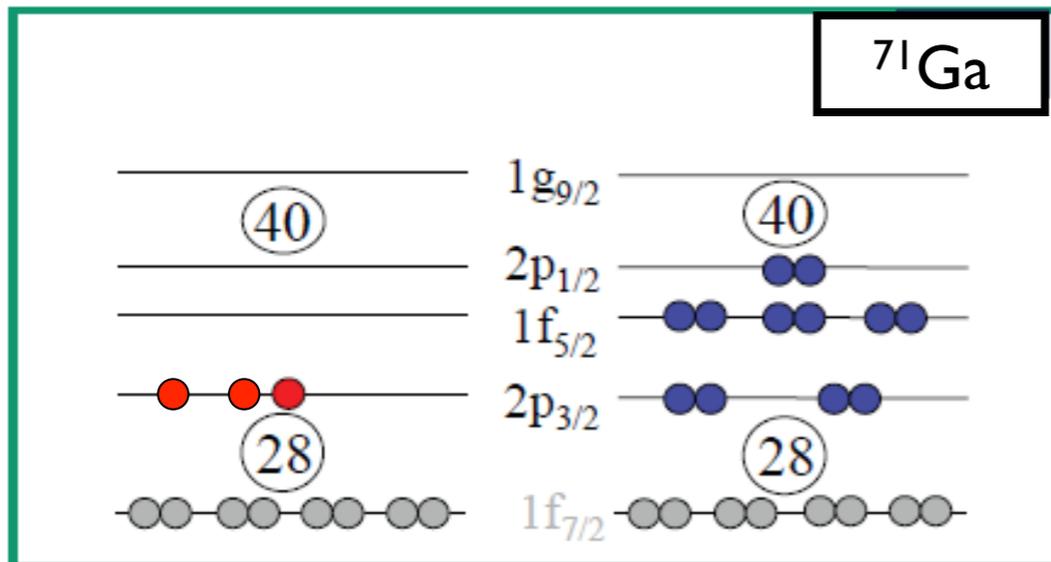
It is these which match actual gs properties ($f^3_{5/2}$ dominated)

Gallium isotopes - charge radii



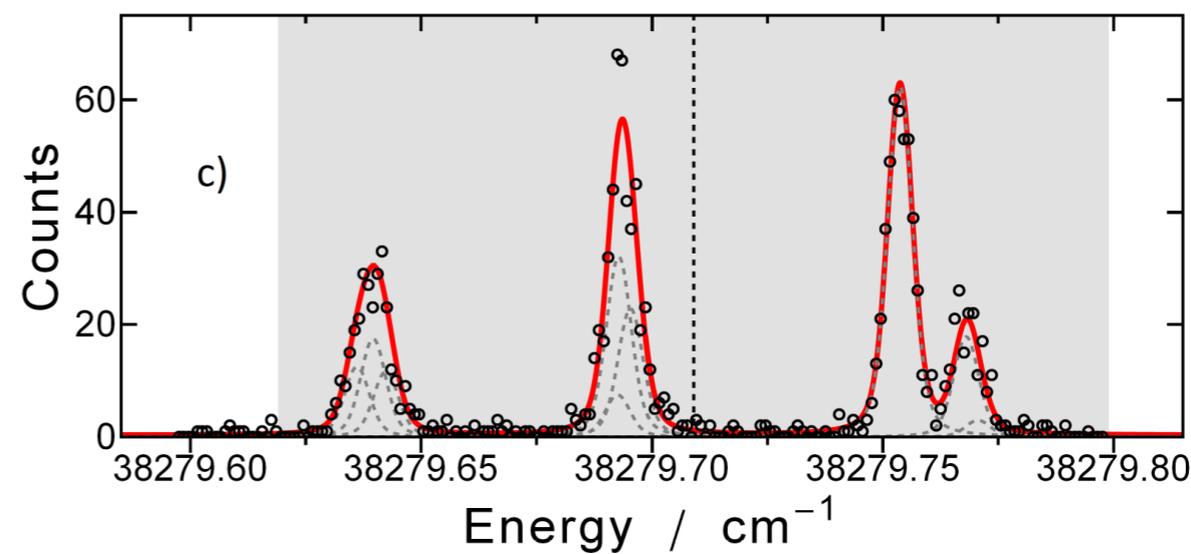
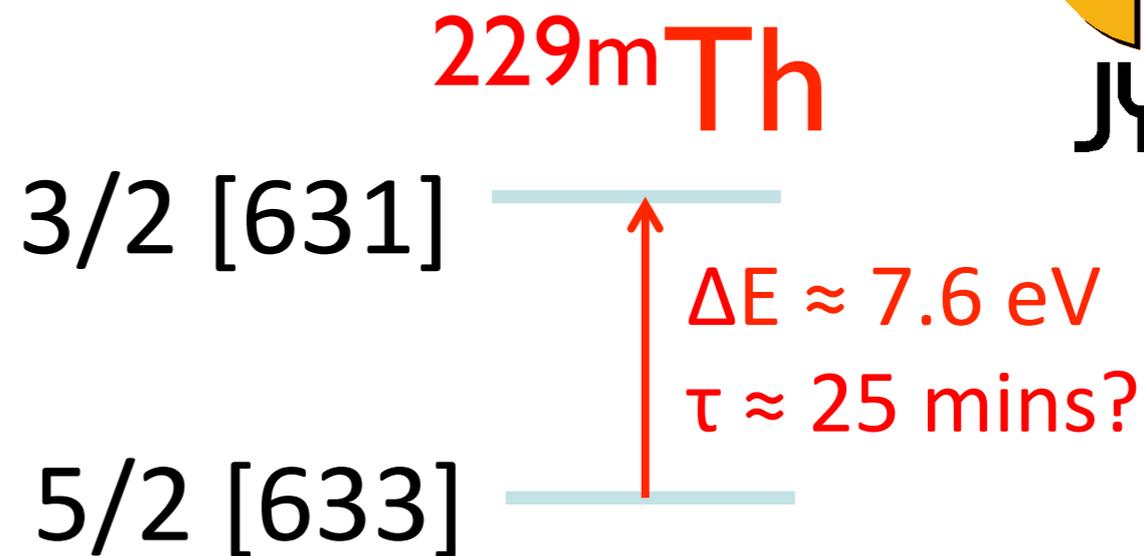
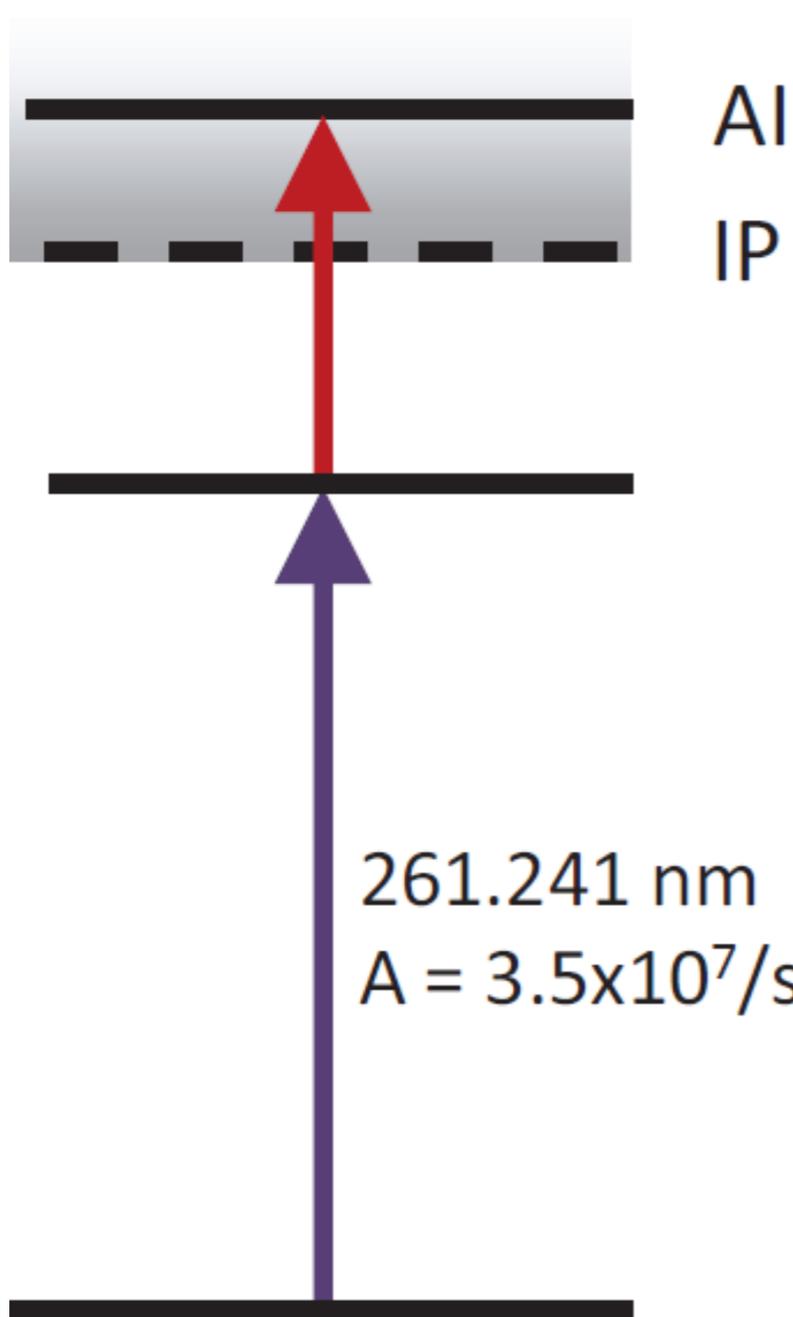
Matter radii of light isotopes – proton skin?

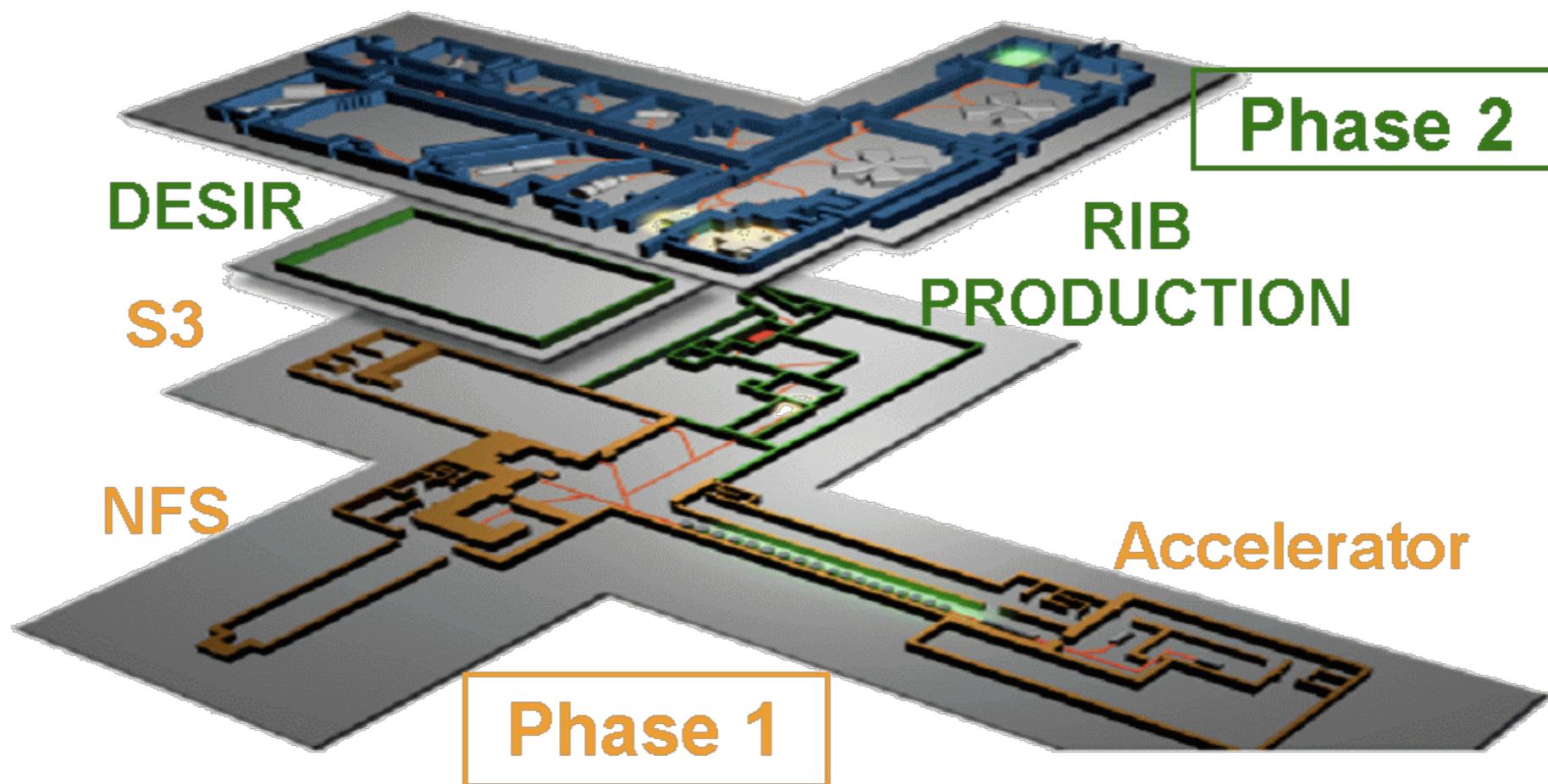
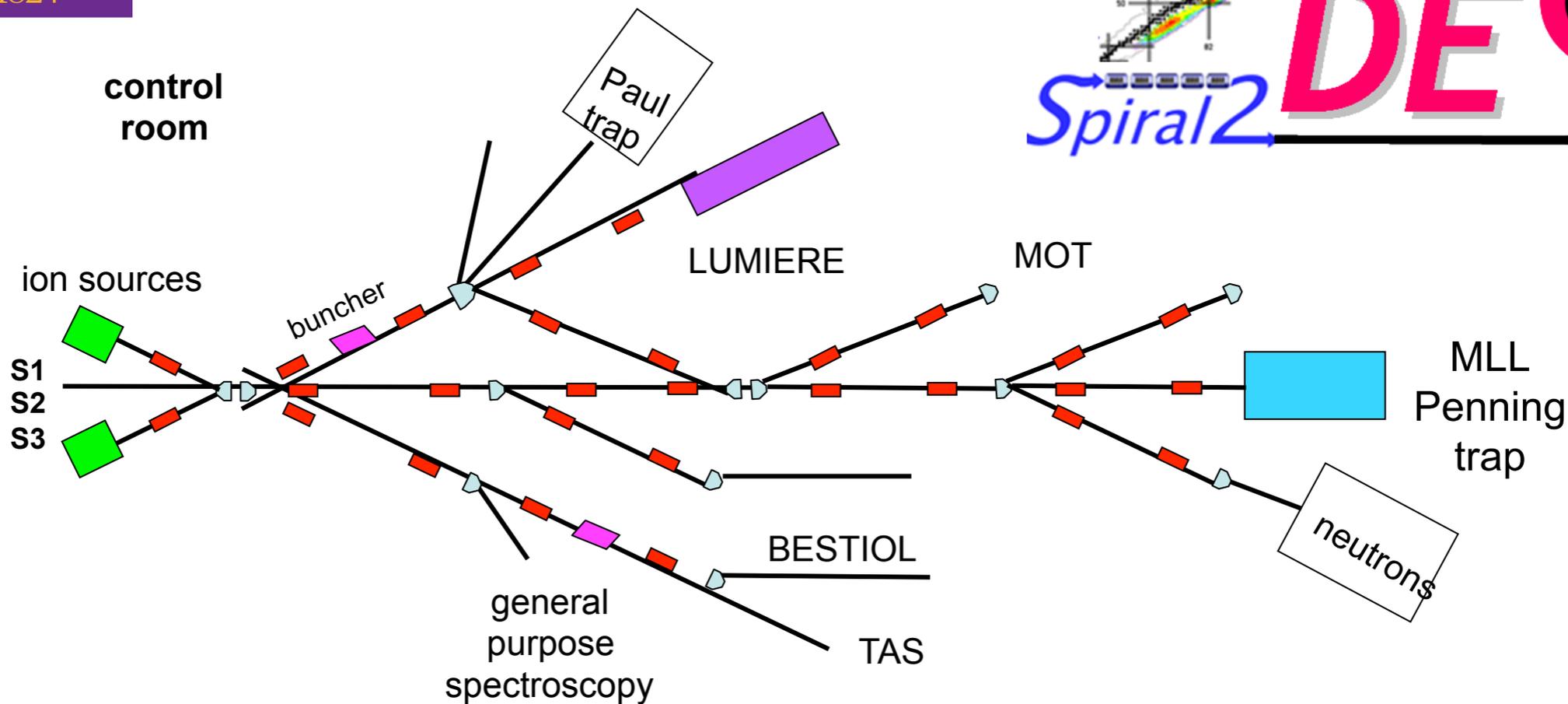
Lépine-Szily et al. Eur. Phys. A **25** (2005) 227



No anomalous effects in the proton charge radii for light isotopes

Hyperfine structure of atomic ^{229}Th





GANIL: HELIOS

Heavy Element Laser Ionization Spectroscopy

- Production of the heavy elements: heavy-ion fusion evaporation reactions
- Separation of the primary and secondary beam: e.g. S3-GANIL
- Thermalization in the gas cell
- Repelling unwanted ions
- Formation of a cooled atomic beam through e.g. a 'de Laval' nozzle (gas jet)
- Resonant laser ionization: high-repetition rate laser system (>10 kHz)
- Ion capture and transport in the RF Ion Guide followed by mass separation
- Detection of the ions: radioactivity / ion counting

